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Outline

Graph



Tree



DFS

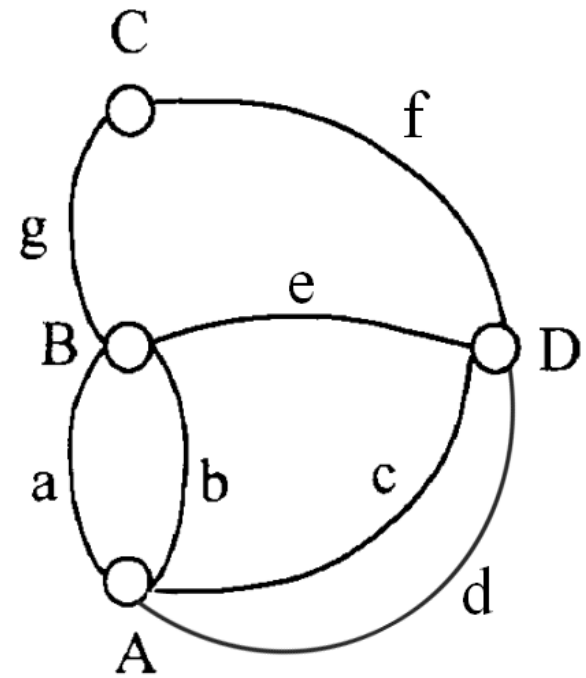


BFS



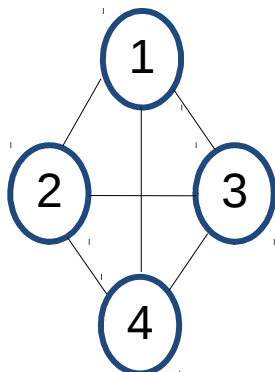
Graph

- Vertex (V)
 - A, D, B, D
- Edge (E)
 - BC, CD, ...
- degree (deg)
 - The Branch of a Vertex
- Path (P)
 - Non-duplicate Vertex Connected Sequence
 - ADCB
- Cycle (C)
 - A Cycle whose Two Ending Points are the same

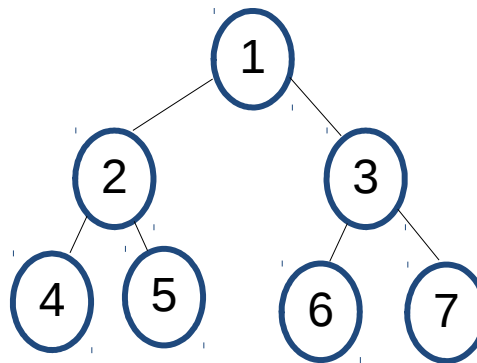


Graph

- Undirected Graph – G1, G2

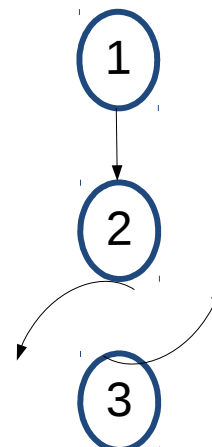


G1



G2

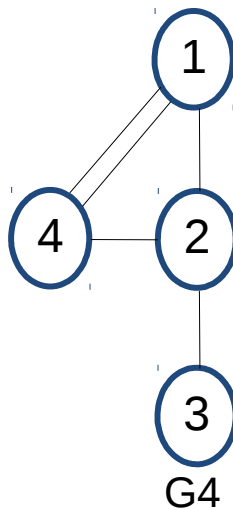
- Directed Graph – G3
 - deg: in-degree and out-degree



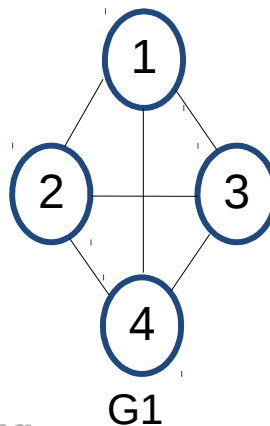
G3

Graph

- Multiple Edge

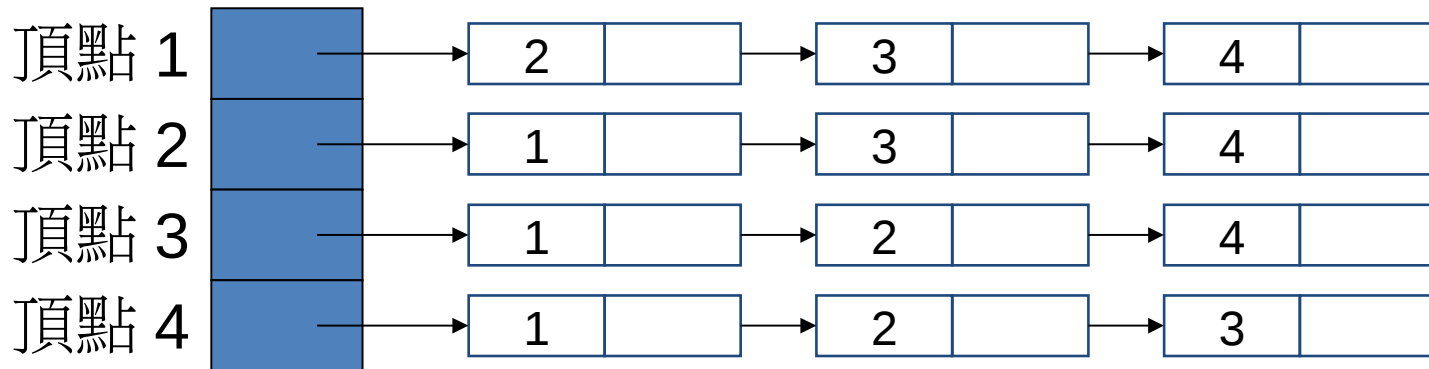
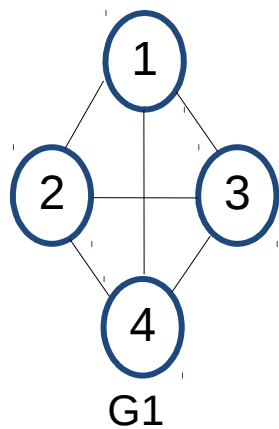


- Complete Graph



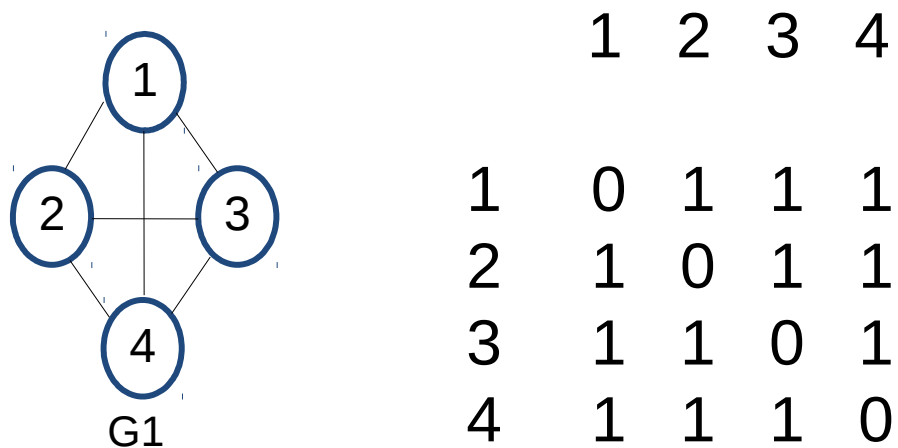
Graph

- Representation
 - adjacent list



Graph

- Representation
 - adjacent matrix



Outline

Graph



Tree



DFS



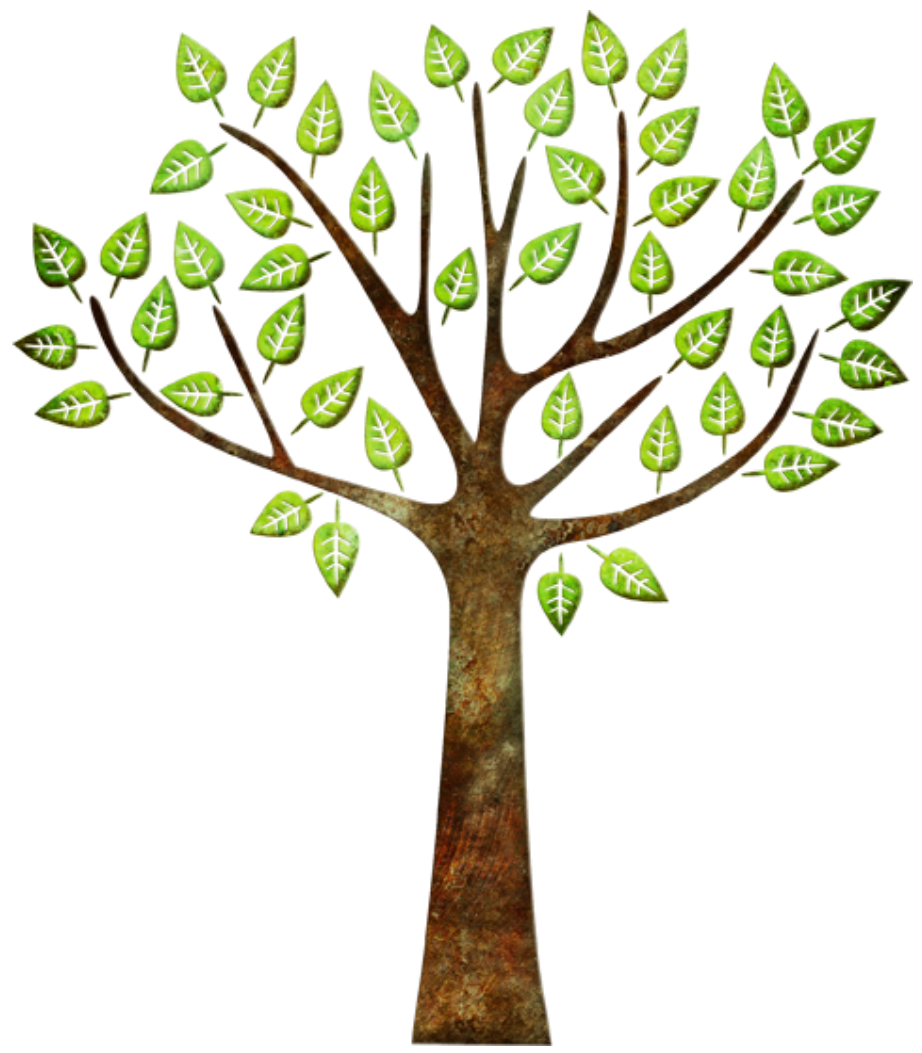
BFS





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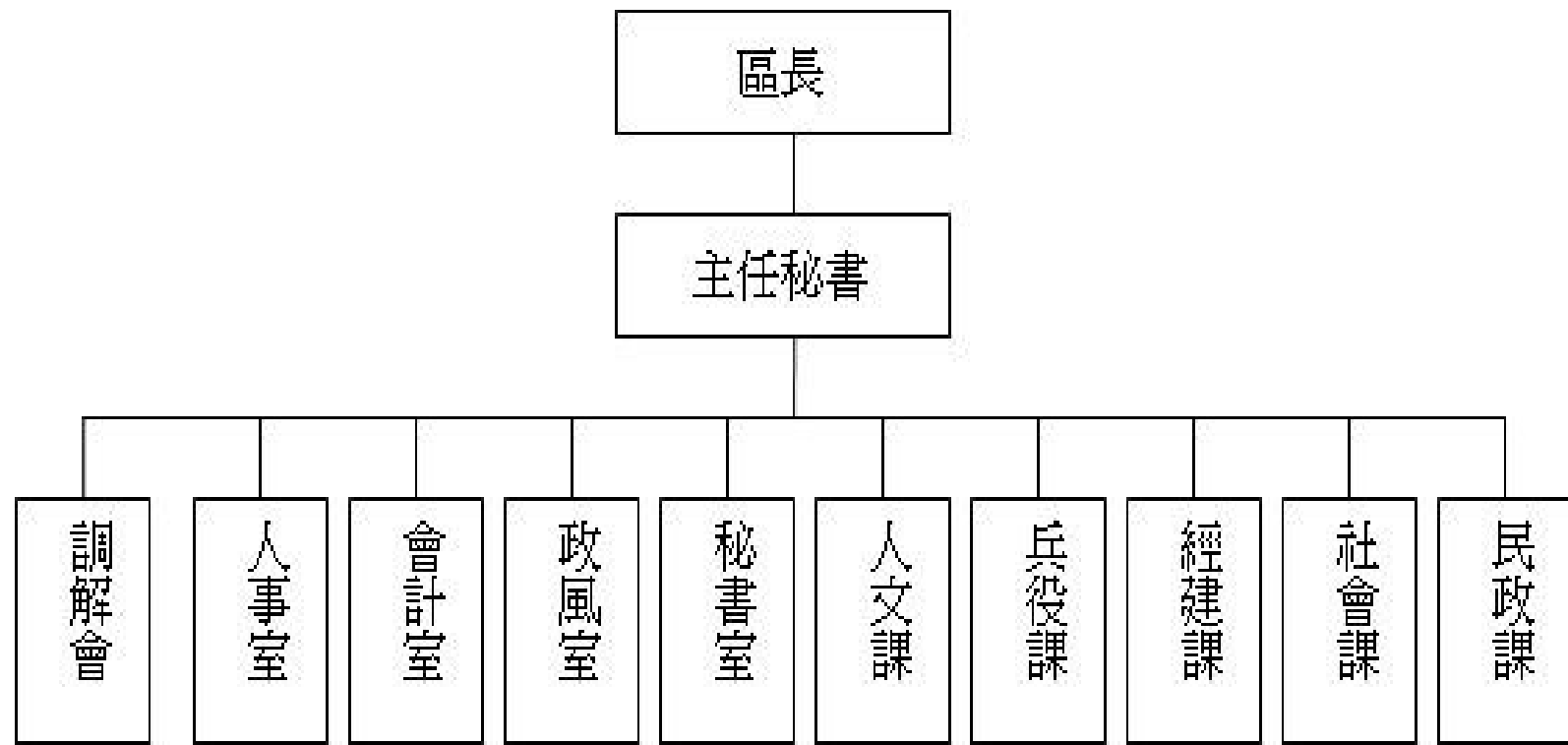


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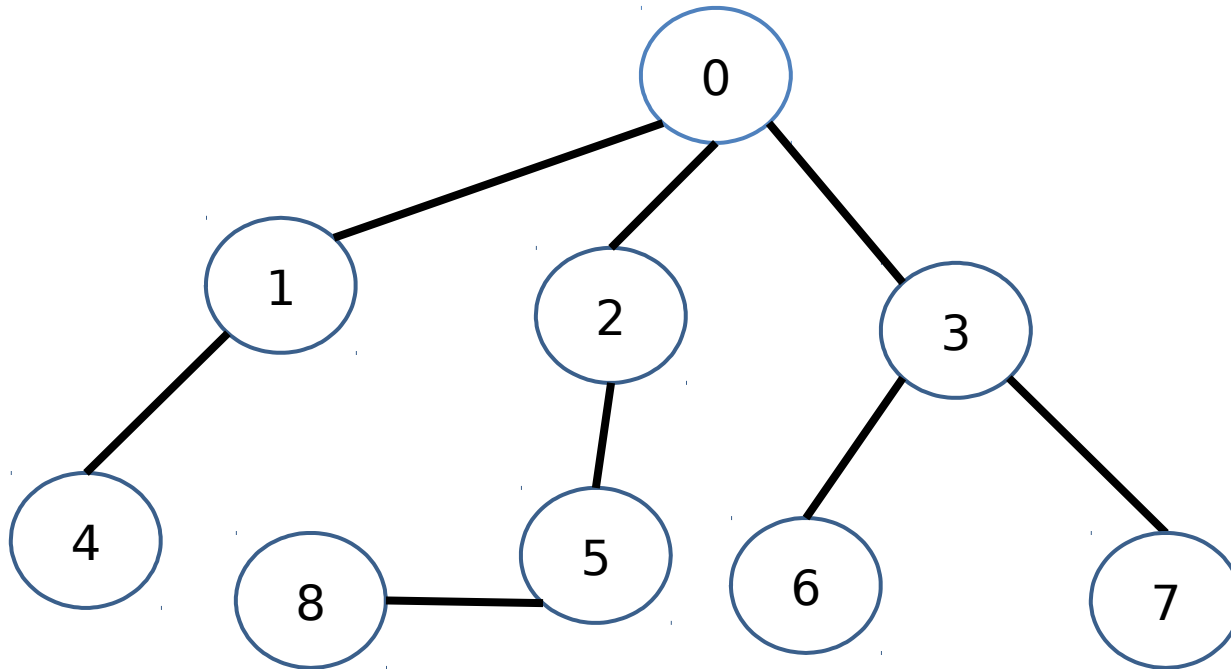
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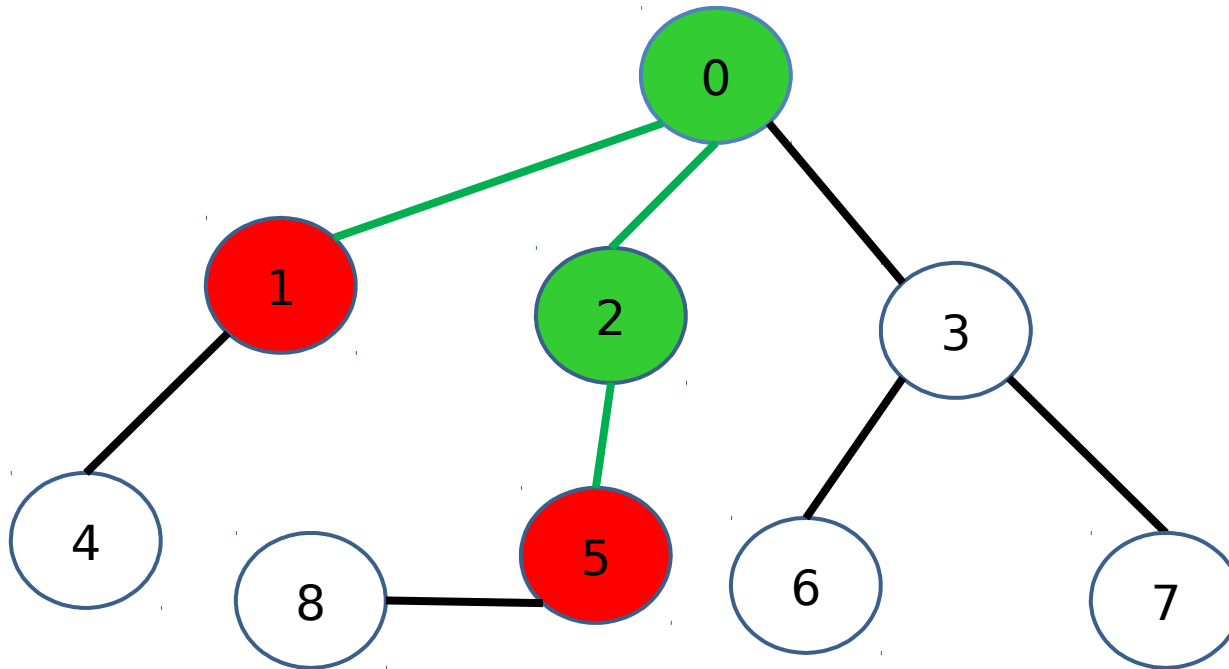
Tree

- A data structure consists of **nodes**. (at least two)



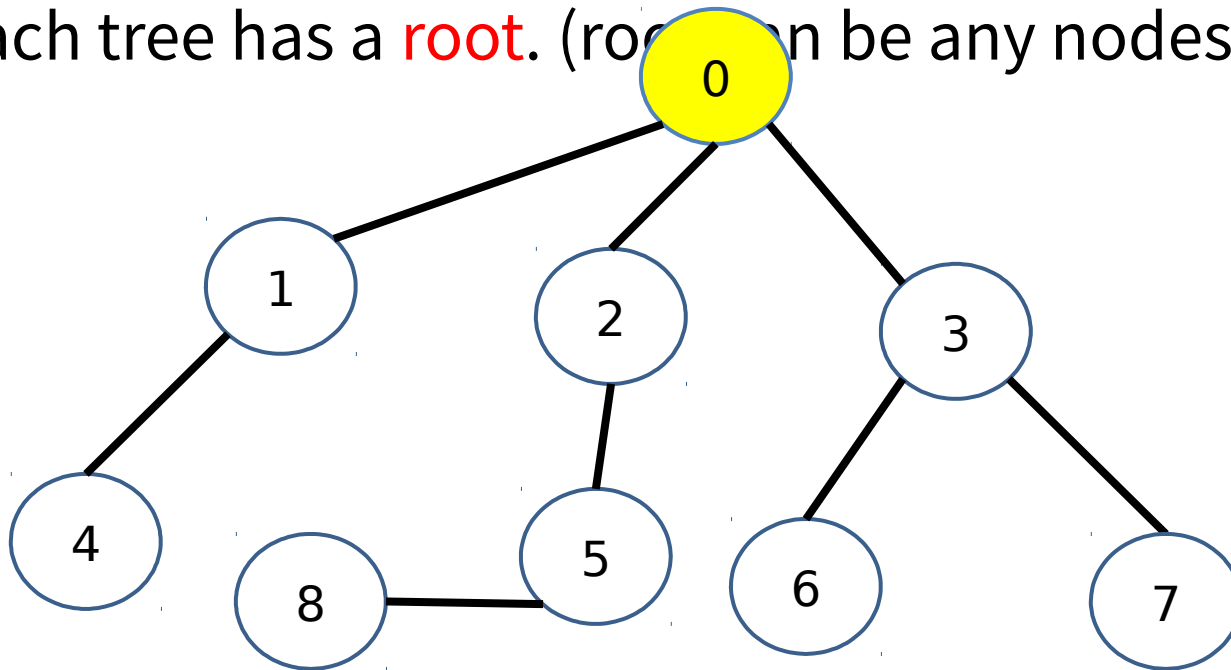
Tree

- A data structure consists of **nodes**. (at least two)
- Every pair of nodes must have **one and only one path**. (connected)



Tree

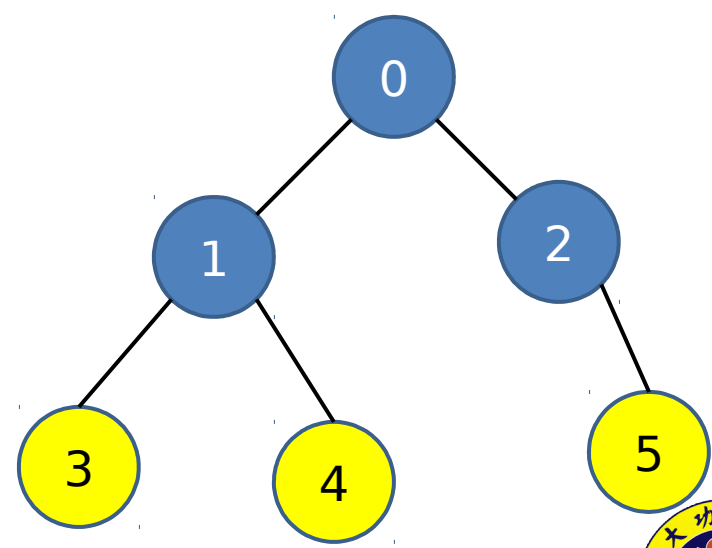
- A data structure consists of **nodes**. (at least two)
- Every pair of nodes must have **one and only one path**. (connected)
- Each tree has a **root**. (root can be any nodes)



Tree

Relations: (using node 0 as root)

-**Leaf:** nodes with no branch. (3,4,5)

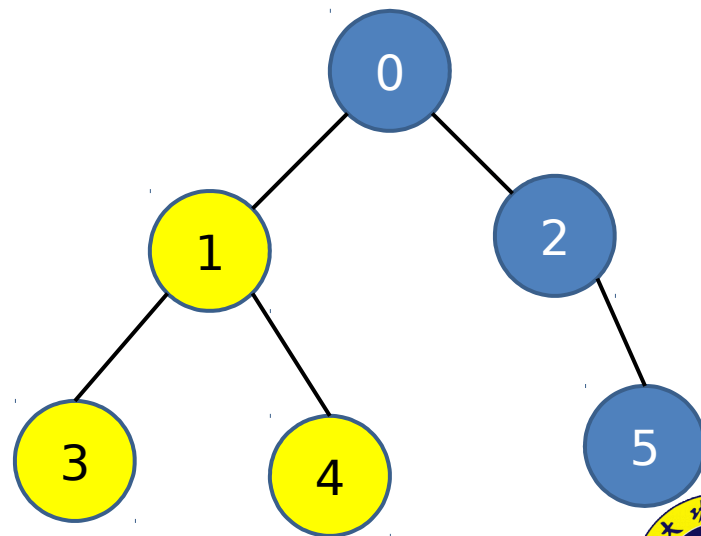


Tree

Relations: (using node 0 as root)

-**Leaf**: nodes with no branch.

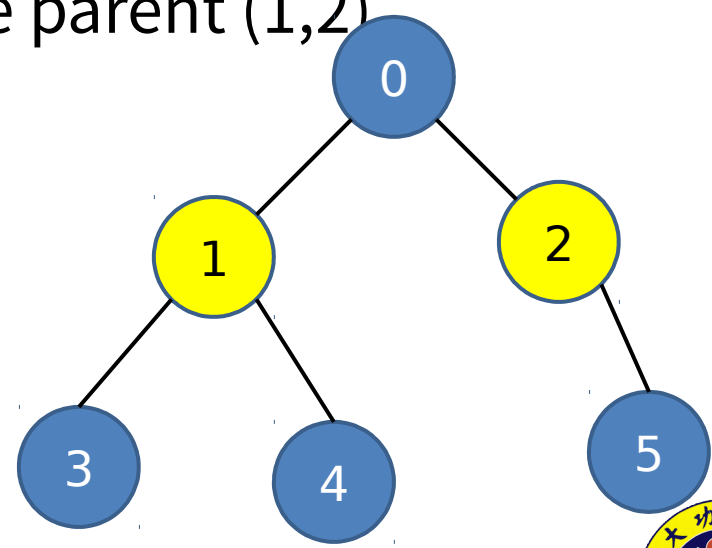
-**Parent/Children**: has successor nodes –Parent (1)
has predecessor node-children (3,4)



Tree

Relations: (using node 0 as root)

- Leaf** : nodes with no branch.
- Parent/Children** : has succesor nodes -Parent
has predecessor node-children
- Sibling**: children with same parent (1,2)



Tree

Relations: (using node 0 as root)

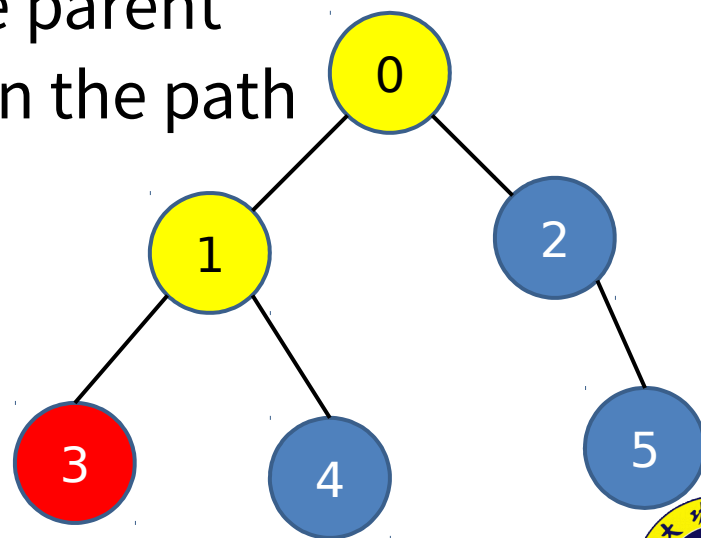
-**Leaf**: nodes with no branch.

-**Parent/Children**: has successor nodes -Parent
has predecessor node-children

-**Sibling**: children with same parent

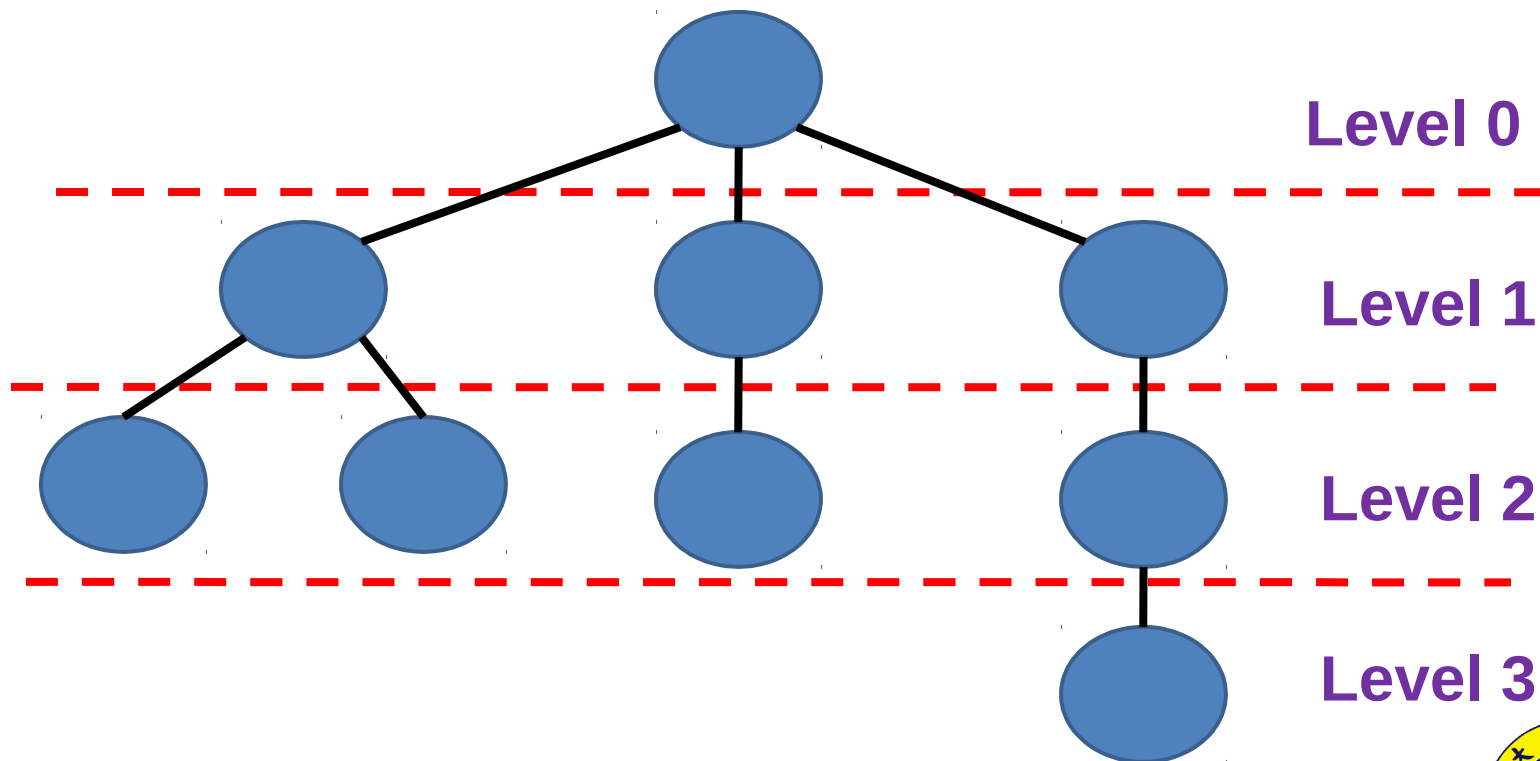
-**Ancestor**: nodes that are on the path
from root to itself.

(3' s ancestor: 0,1)



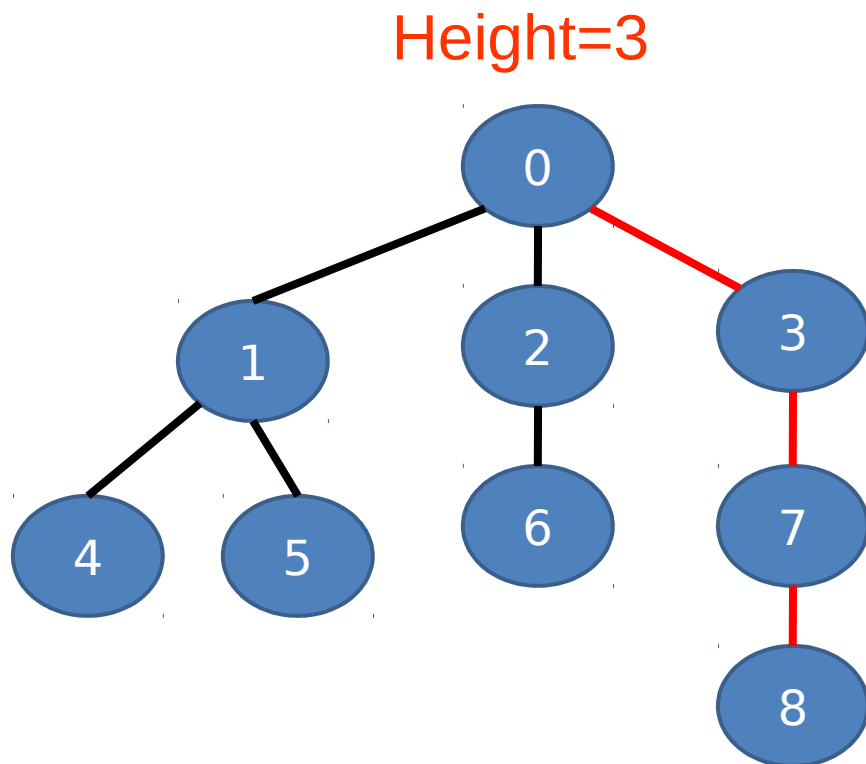
Tree

- **Tree Level:** according to the **distance to the root**.



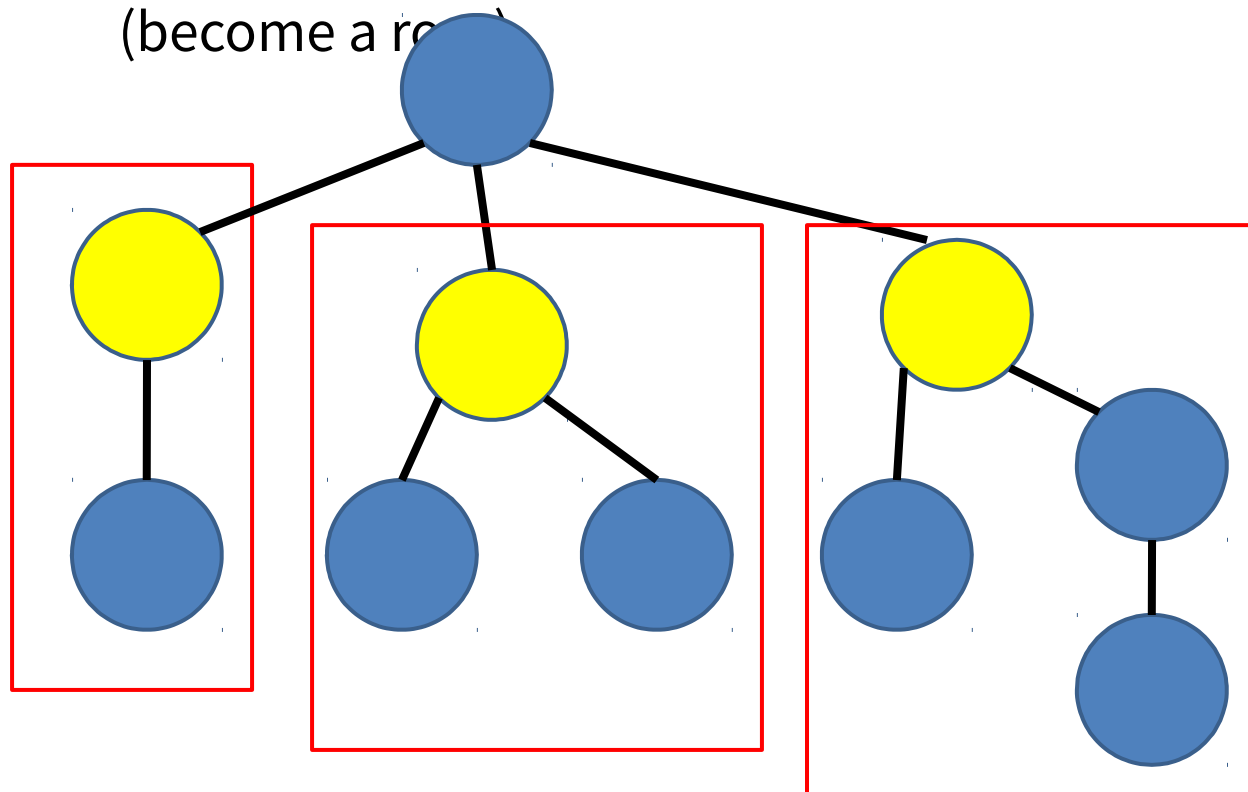
Tree

- **Tree Height(Depth):** the maximum distance from the root.



Tree

- **SubTree:** nodes that are not the root can form a subtree



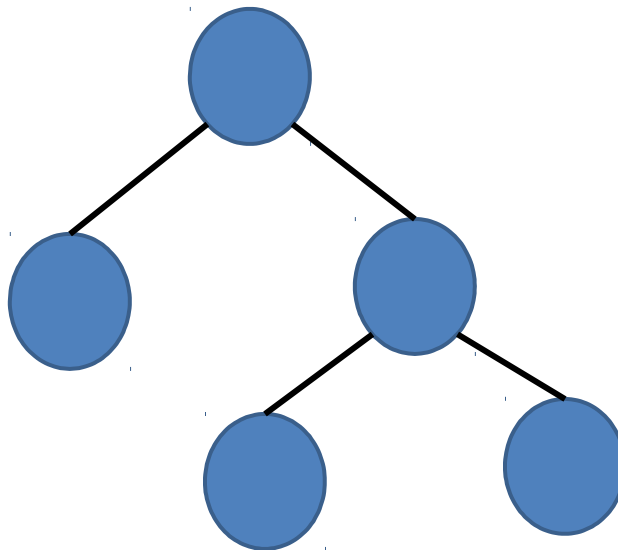
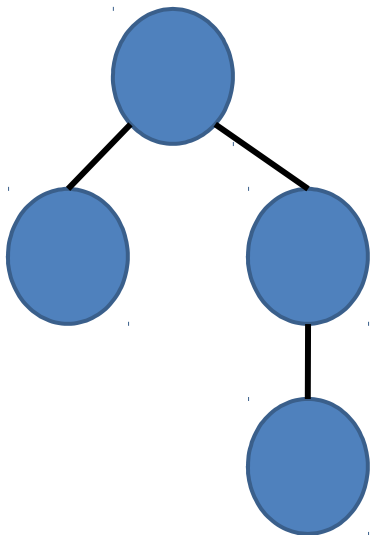
Tree

- **Feature:**
 - no cycle
 - every pair of nodes are connected
 - every pair of nodes has only one path

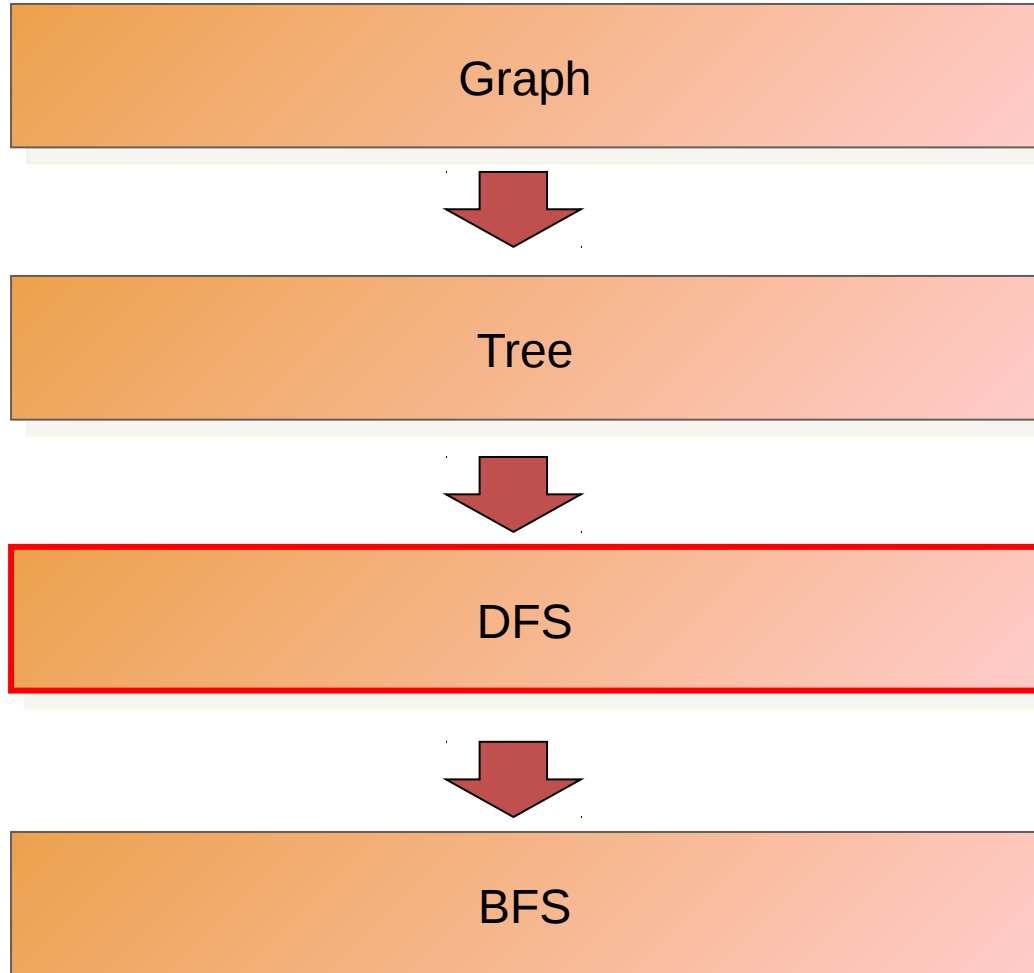


Tree

- **Forest:** n trees are disjoint ($n \geq 0$)
 ☒ can be empty



Outline



DFS

(D)epth-(F)irst-(S)earch



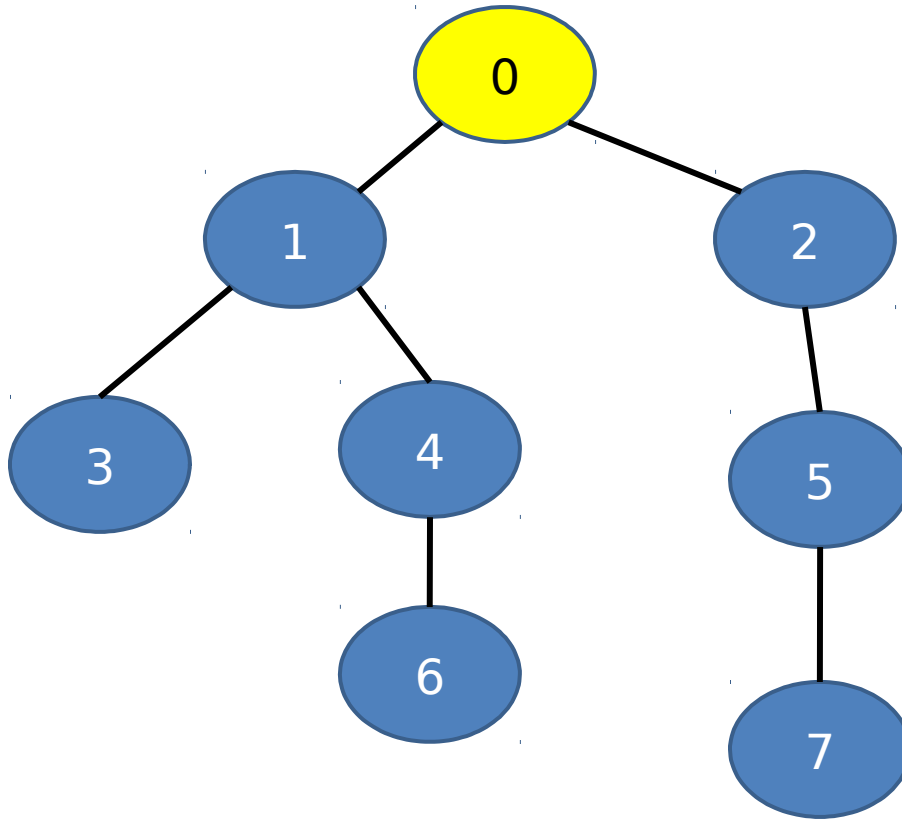
DFS

(D)epth (F)irst (S)earch

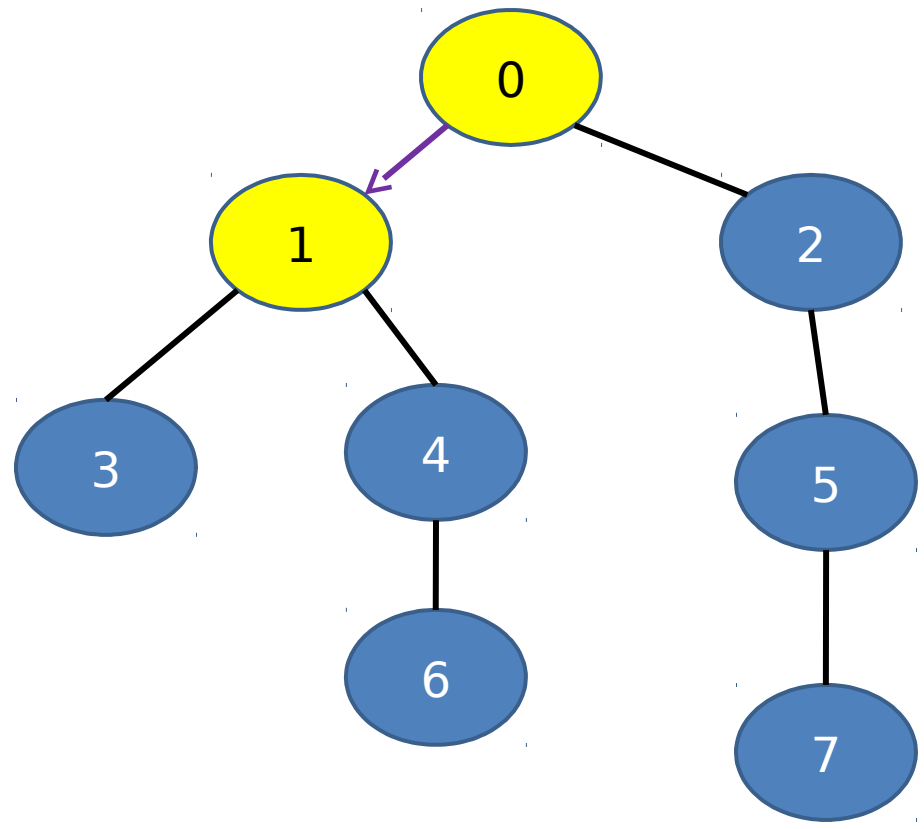
Stack



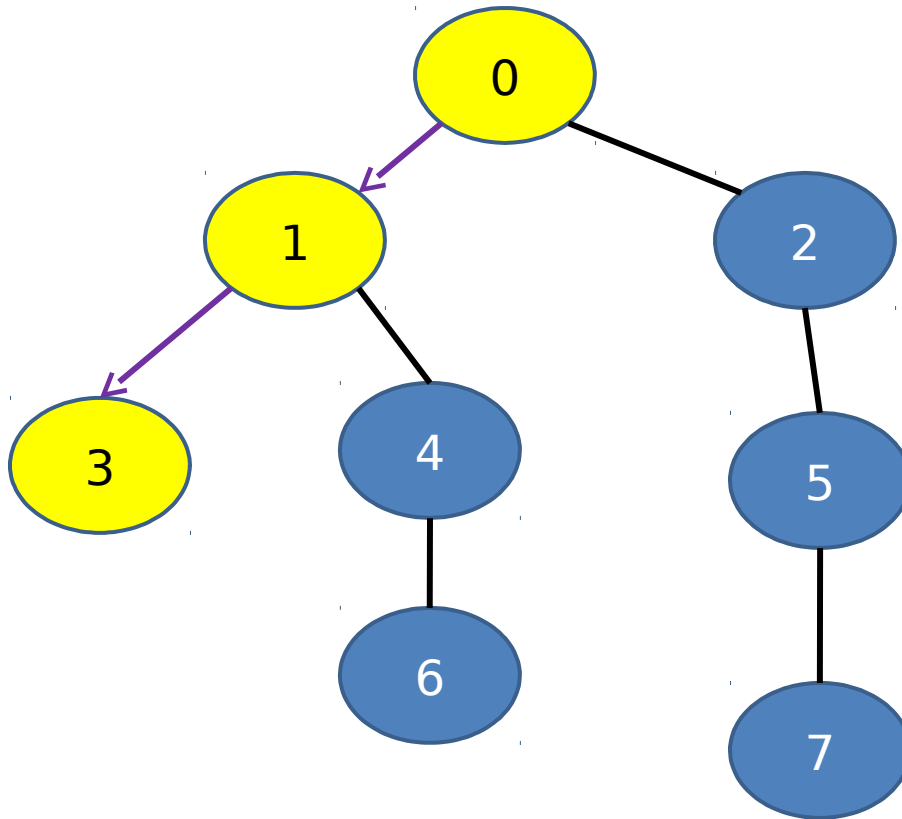
DFS



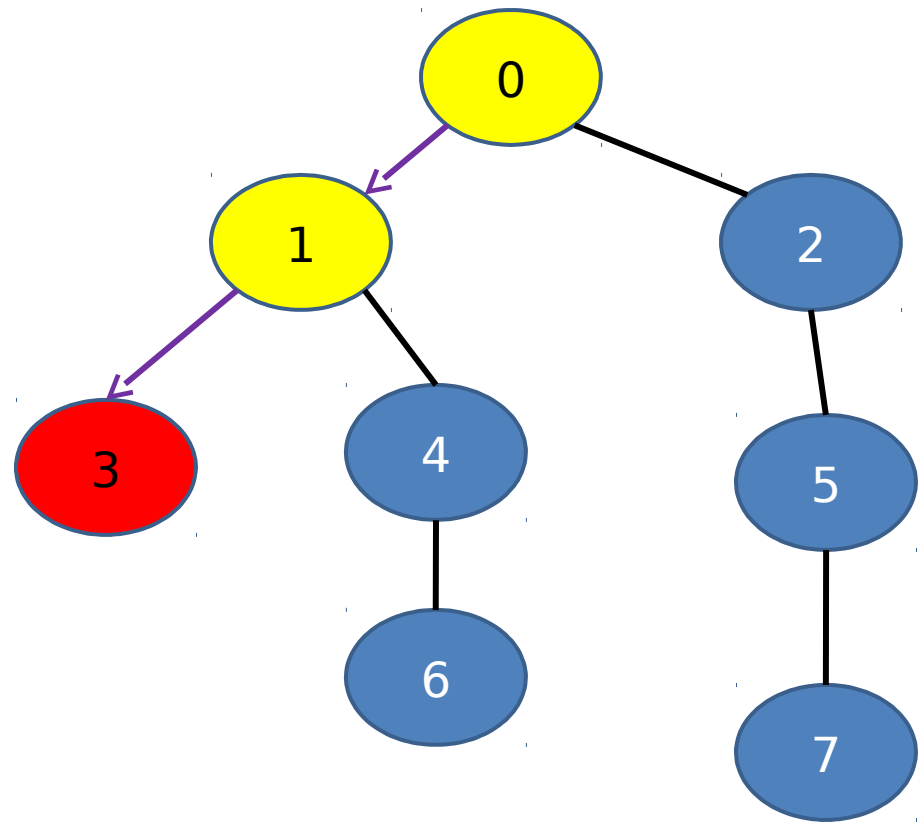
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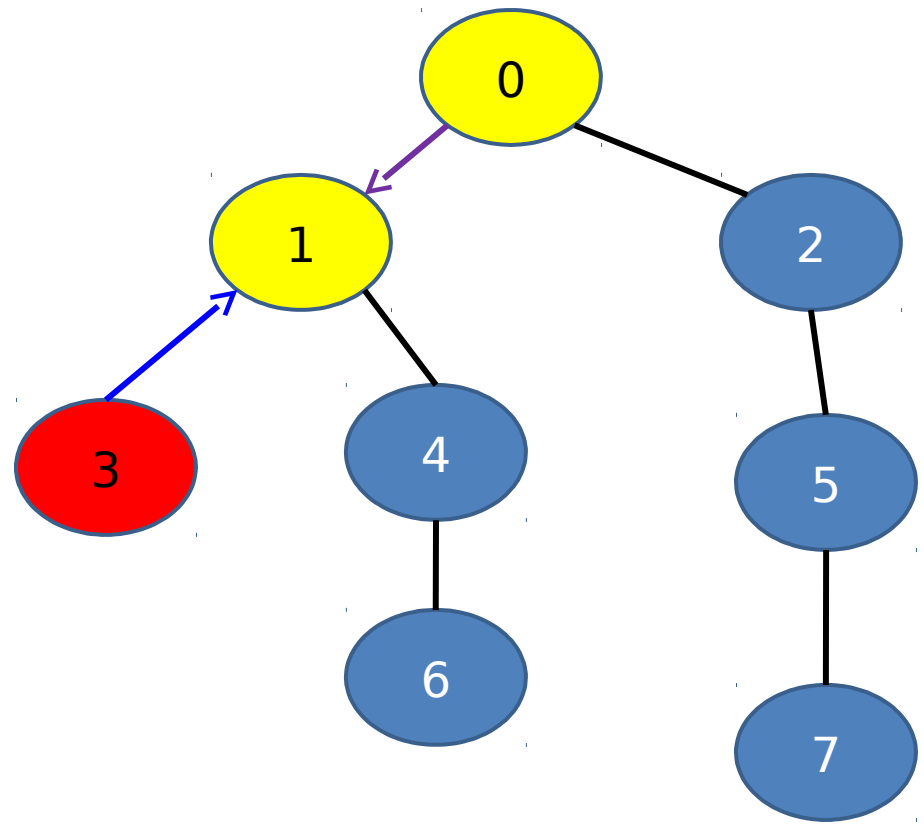
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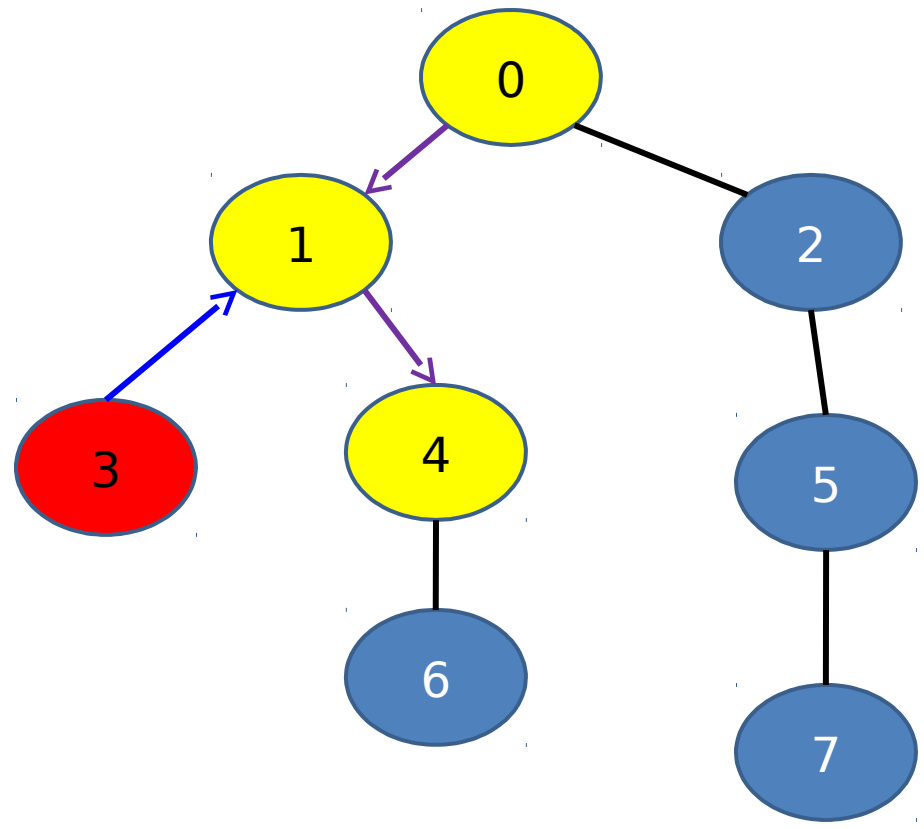
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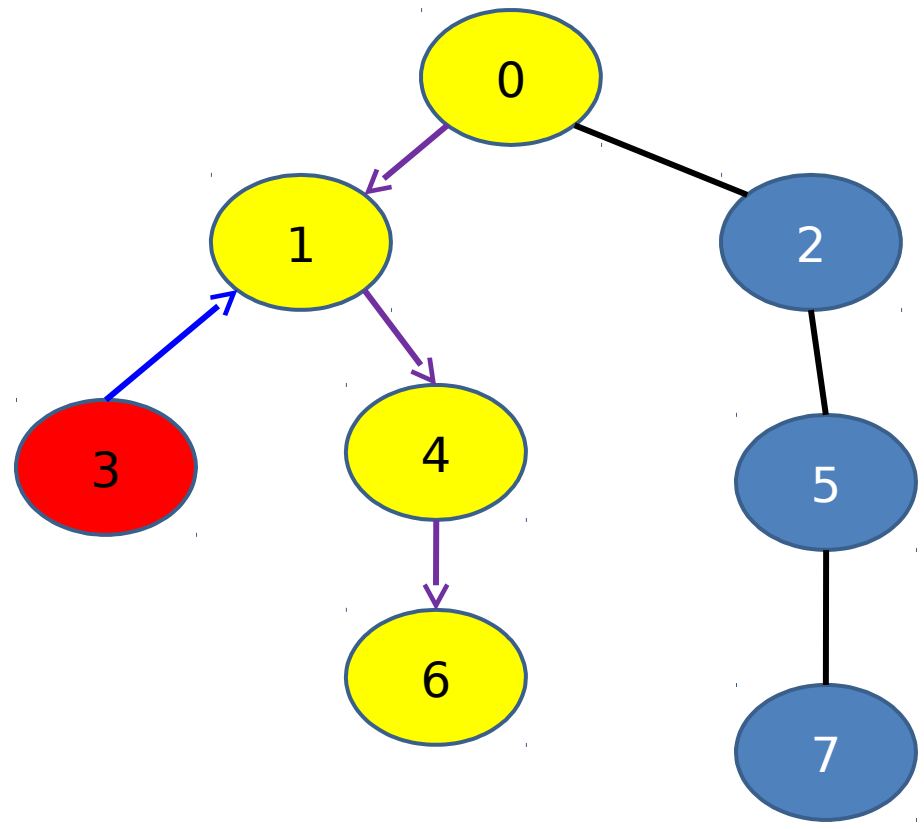
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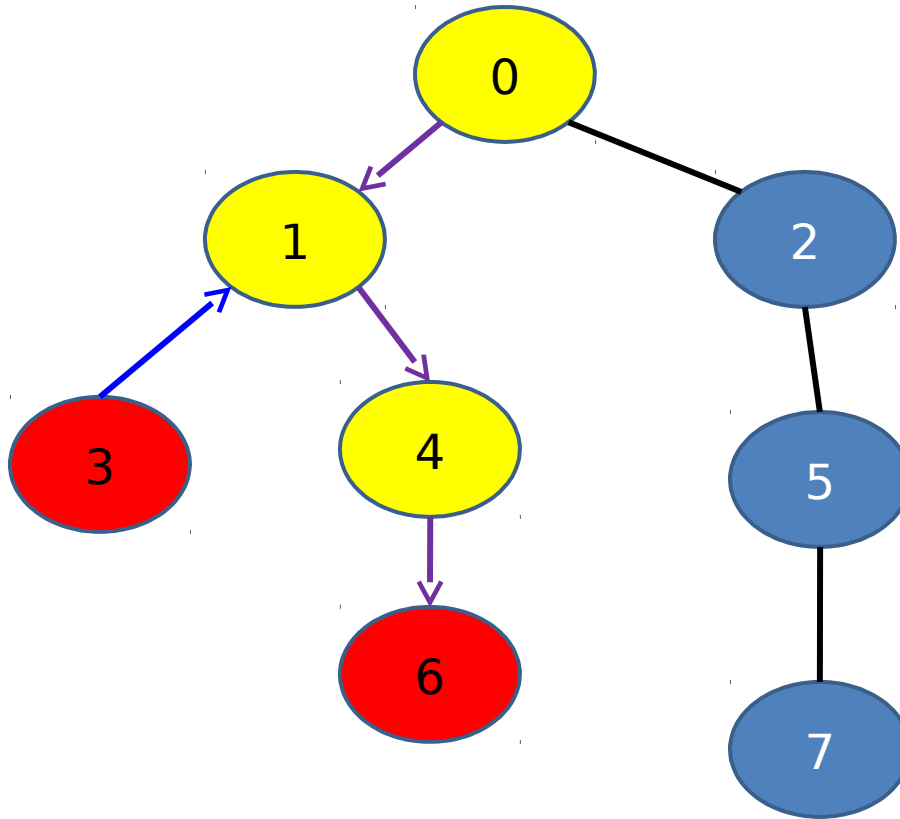
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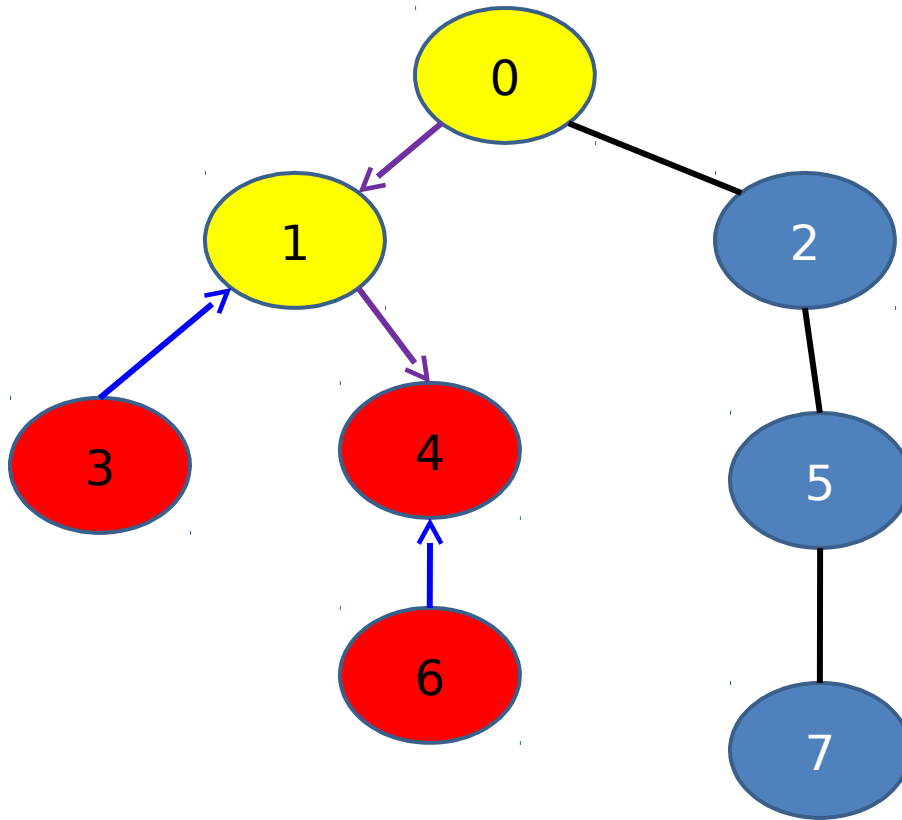
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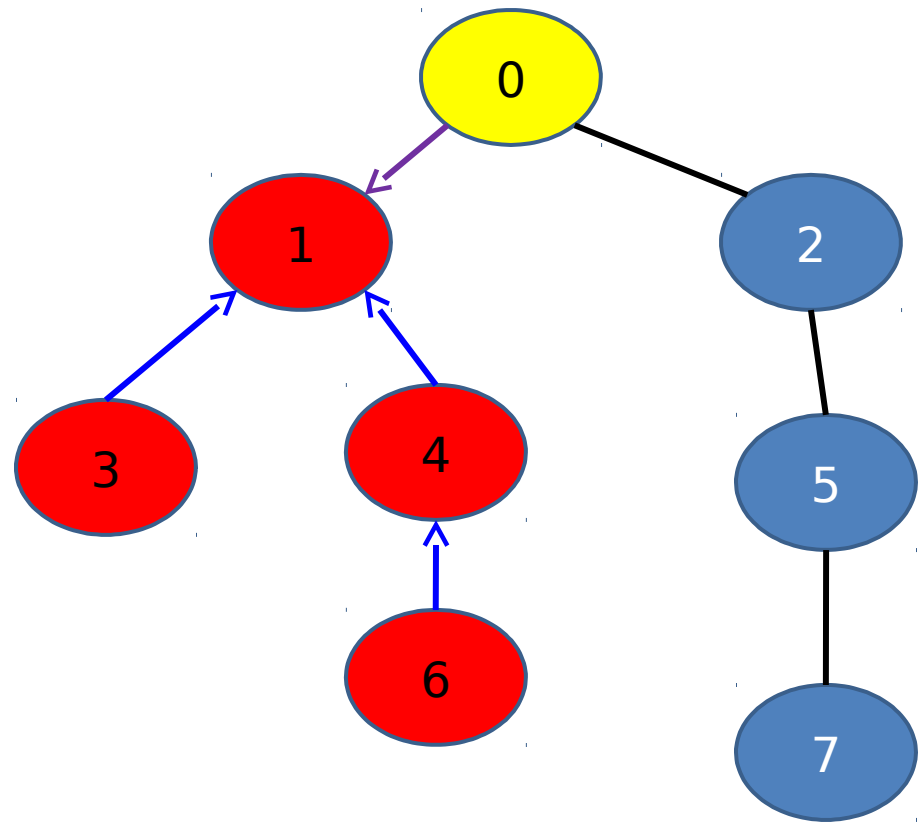
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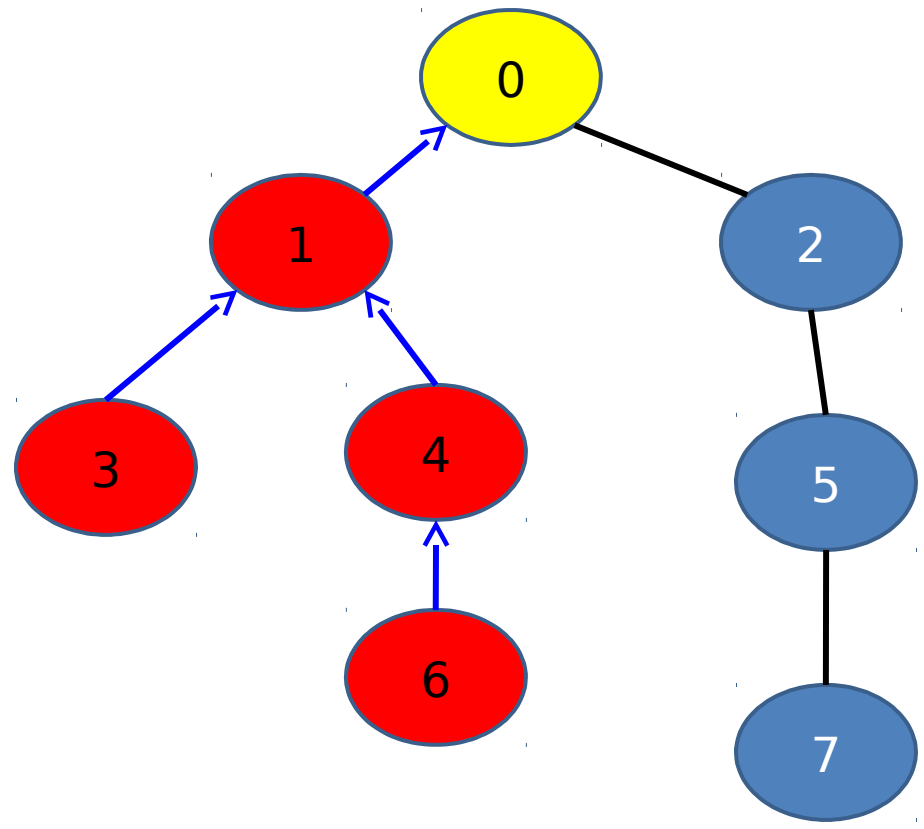
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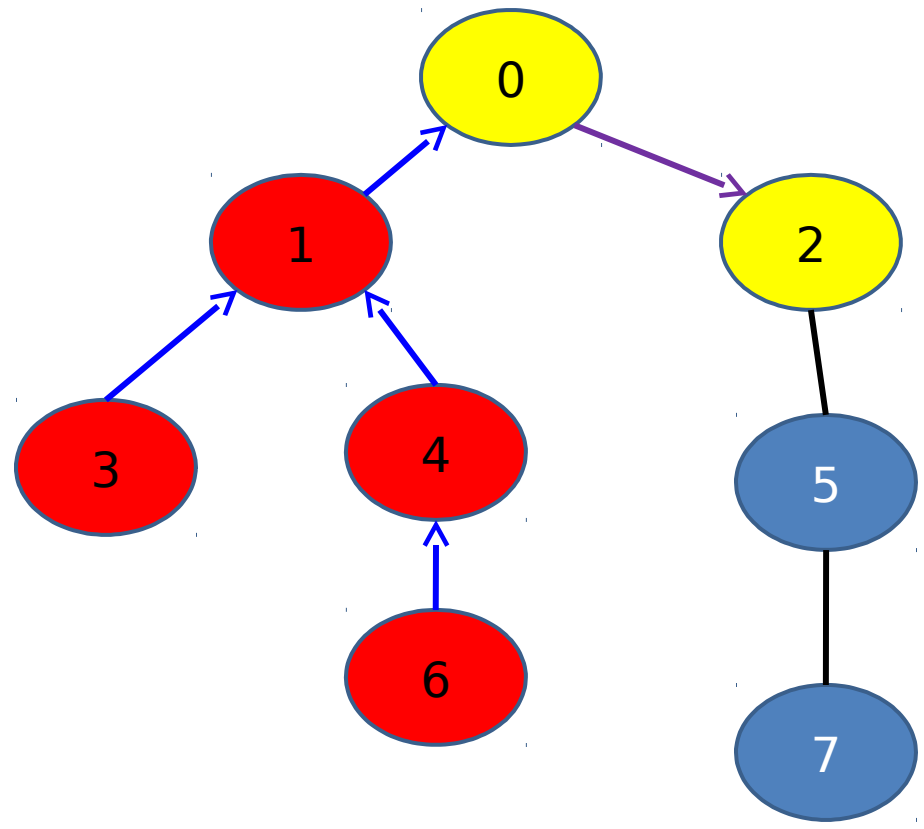
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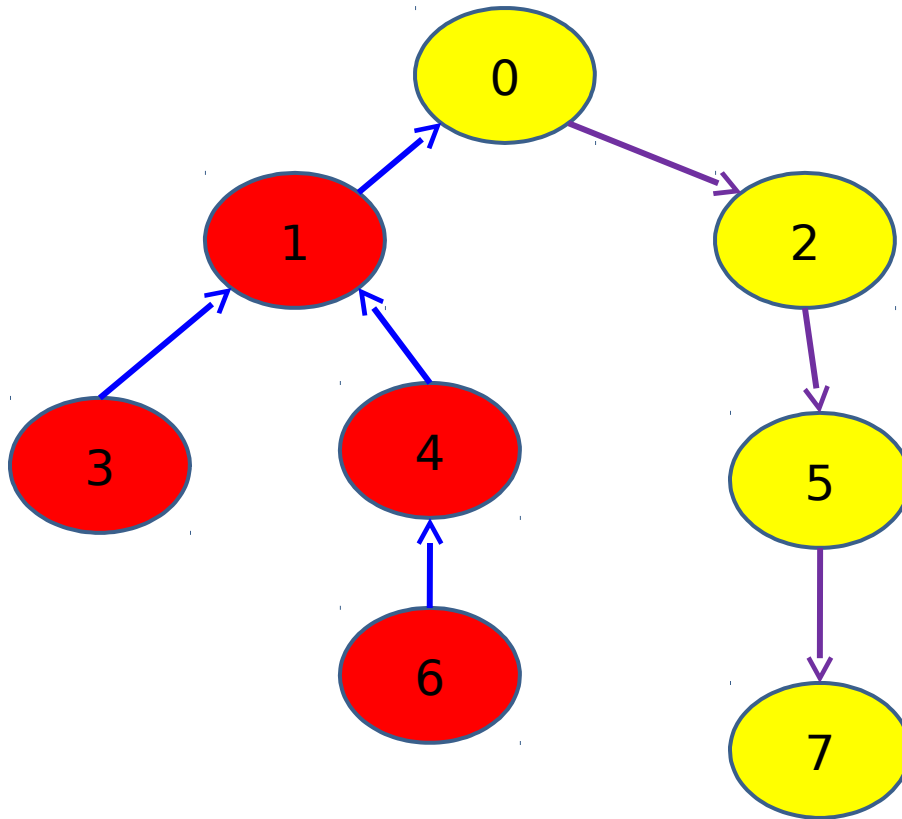
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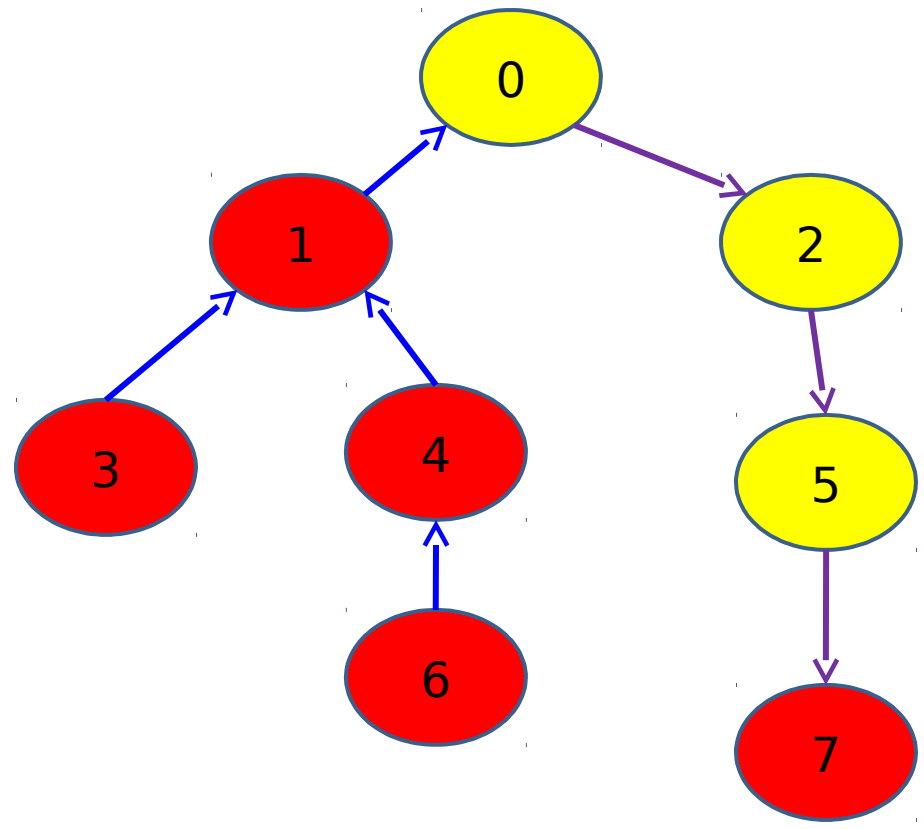
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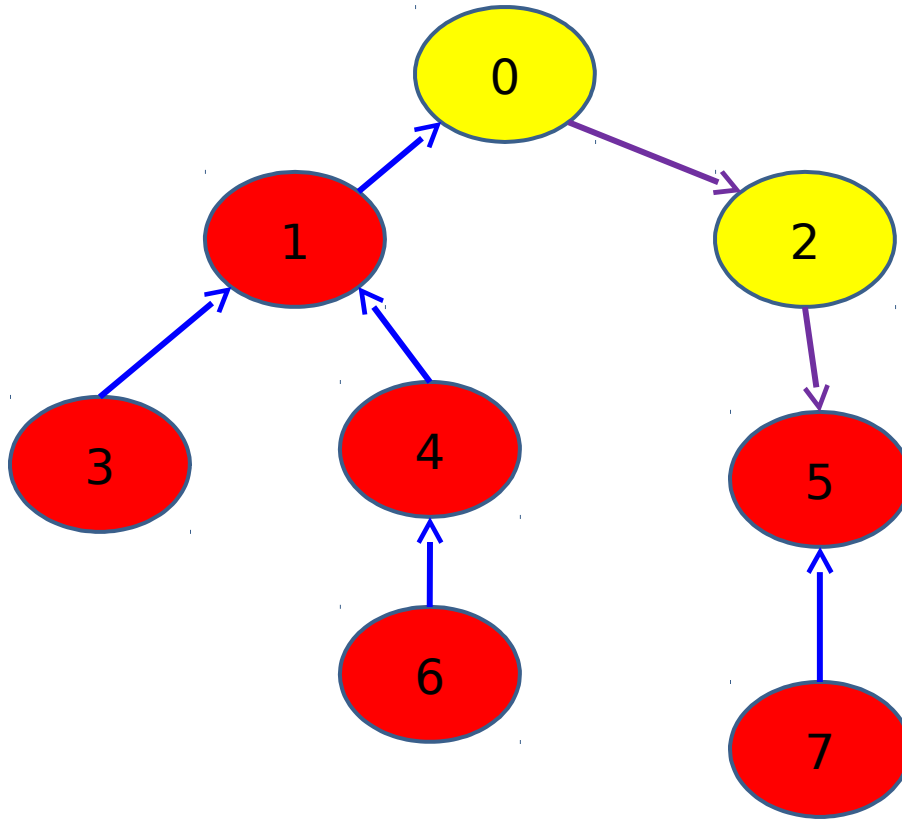
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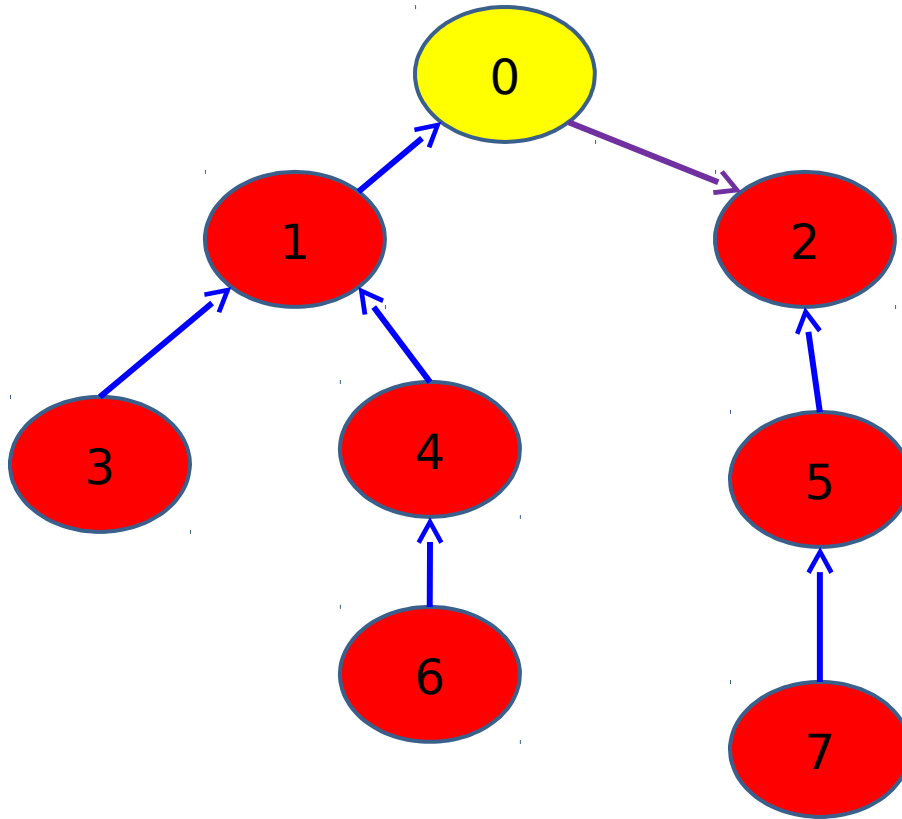
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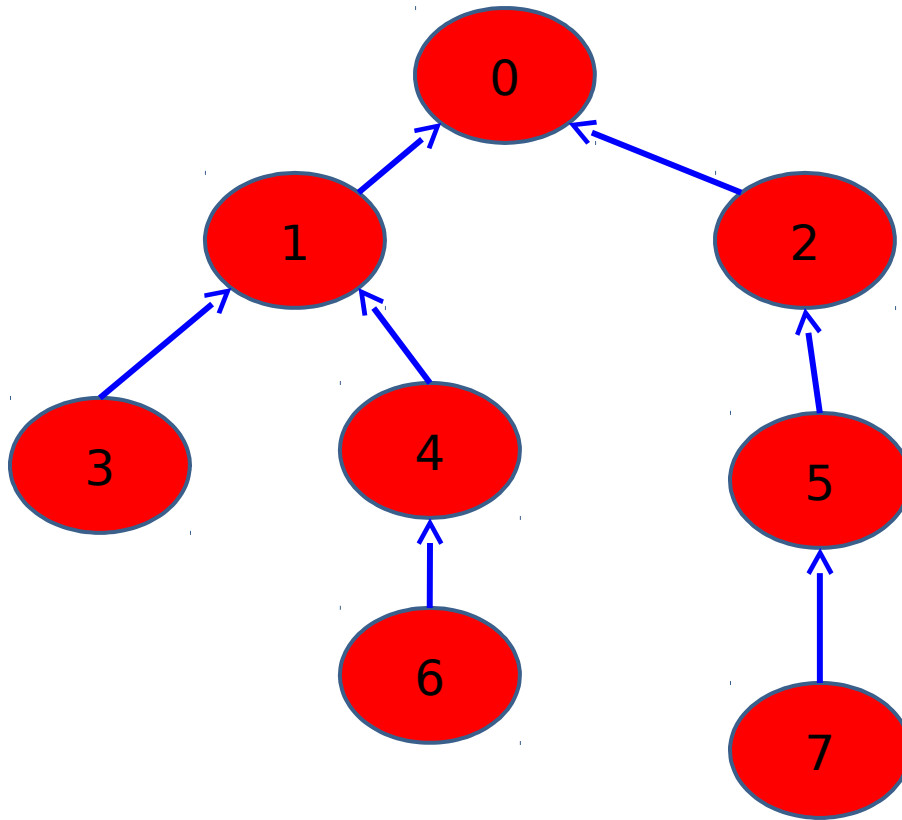
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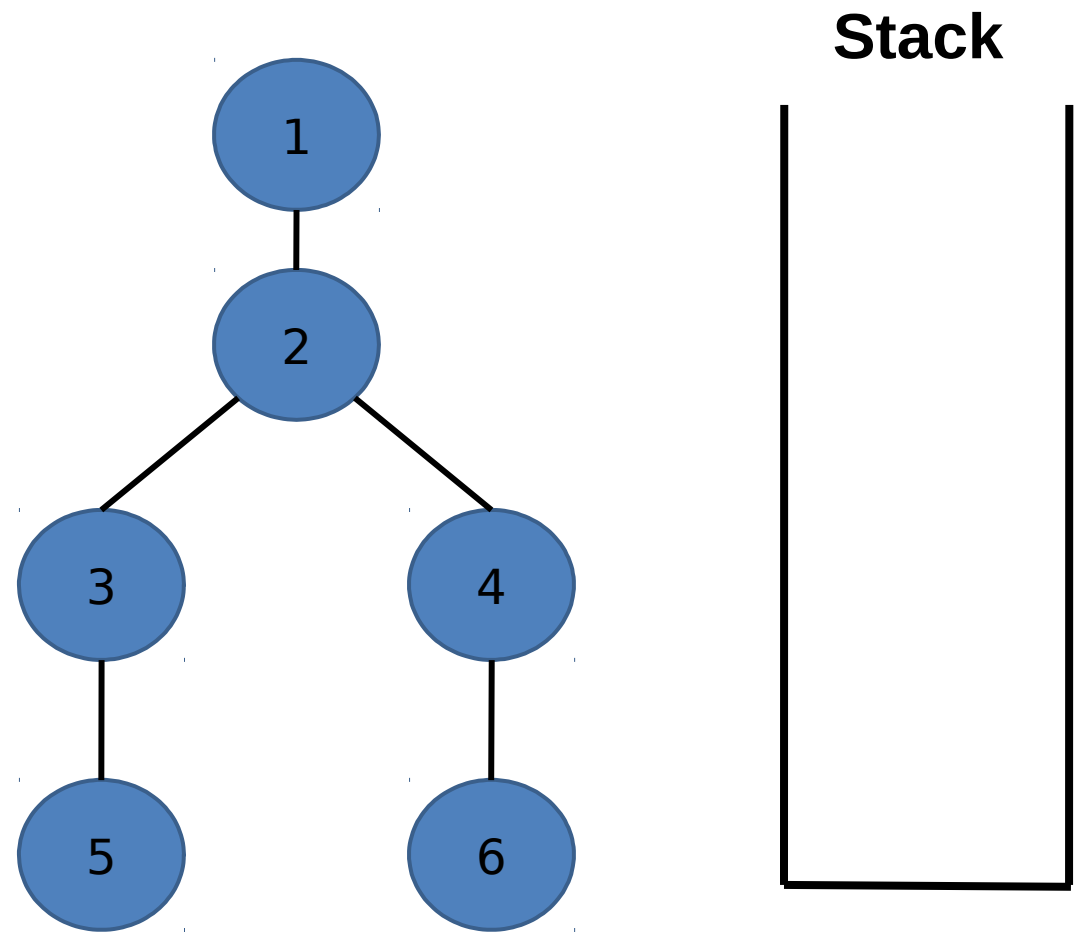
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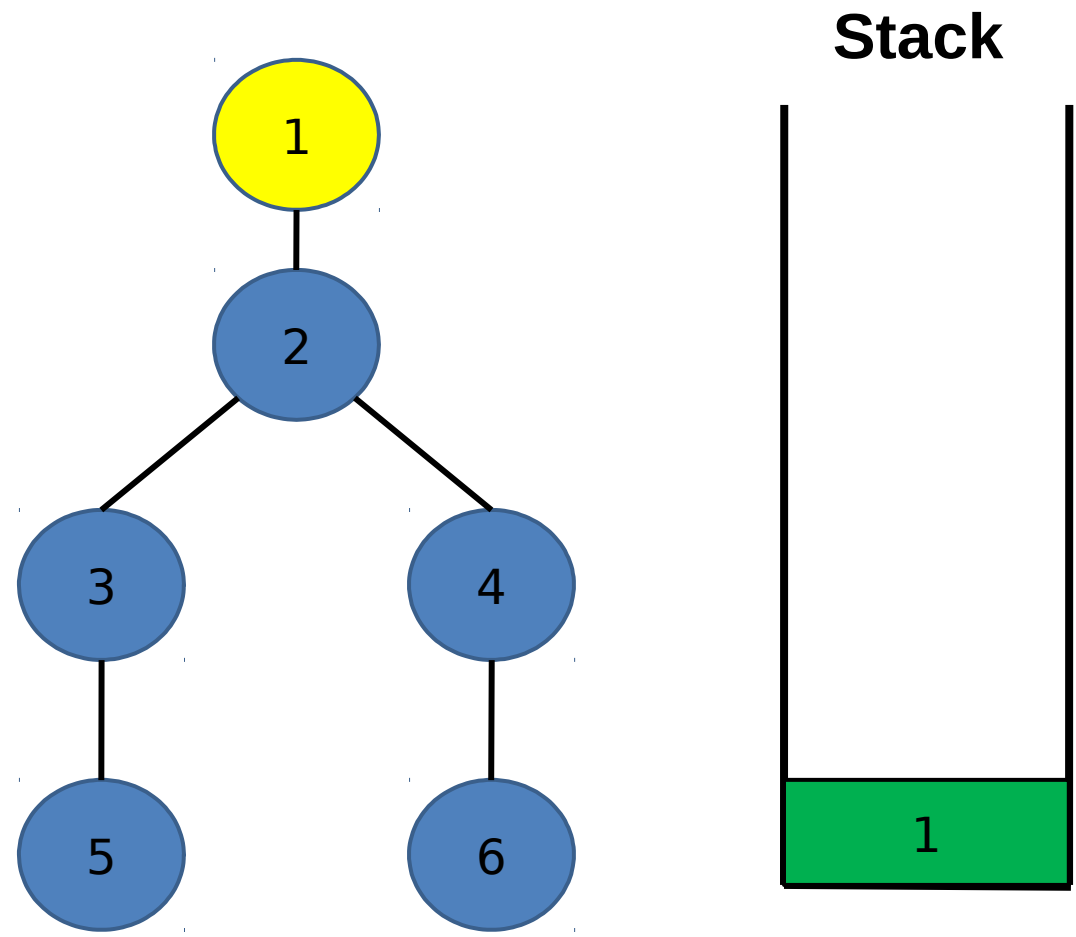
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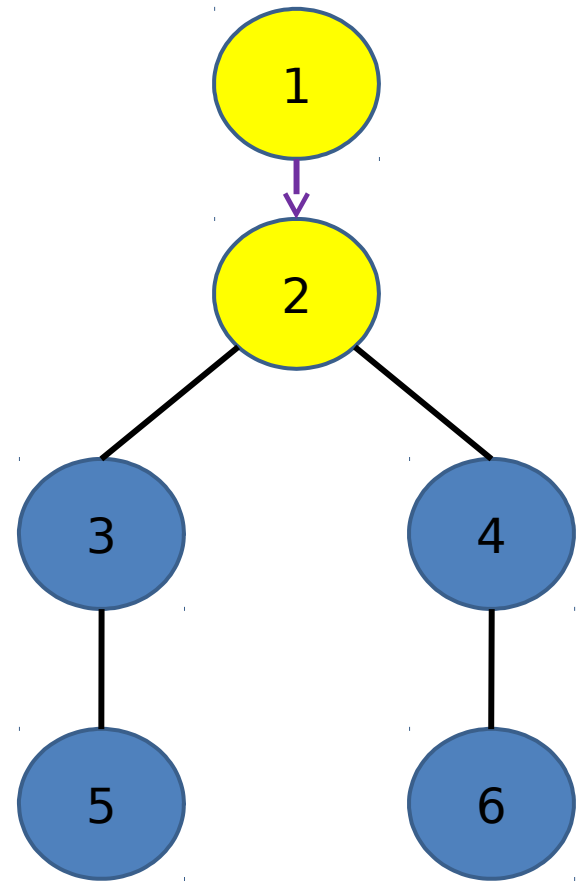
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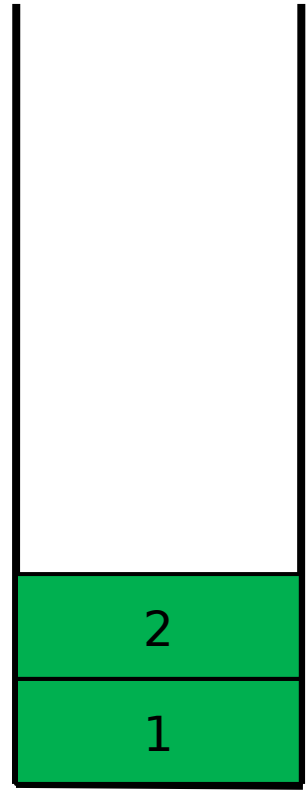
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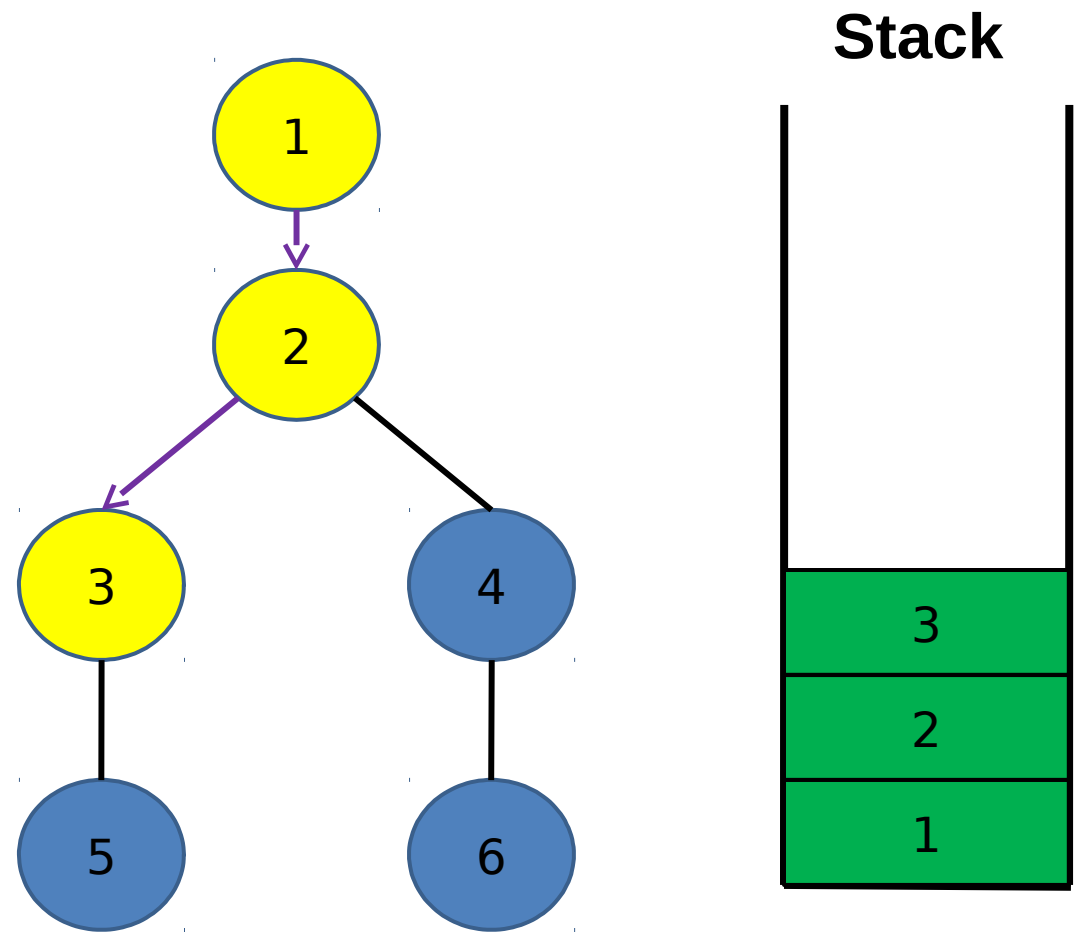
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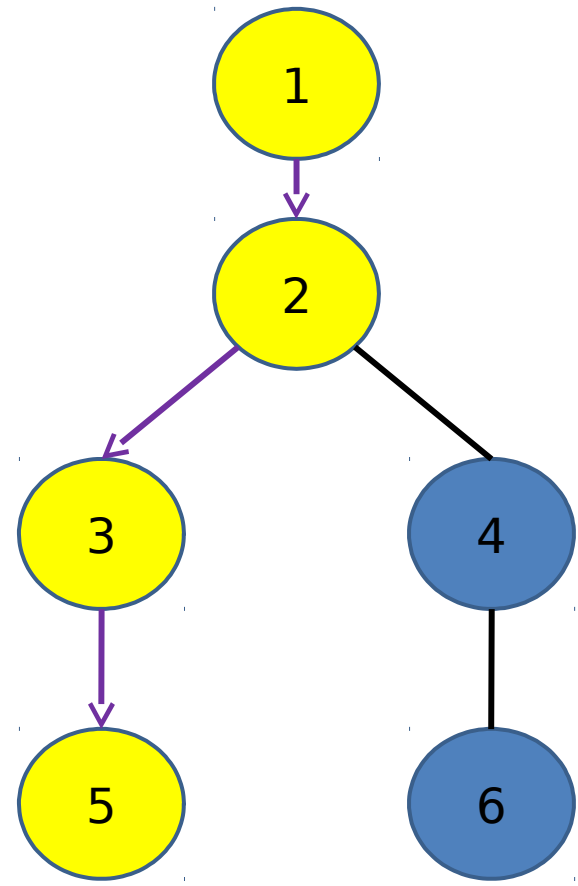
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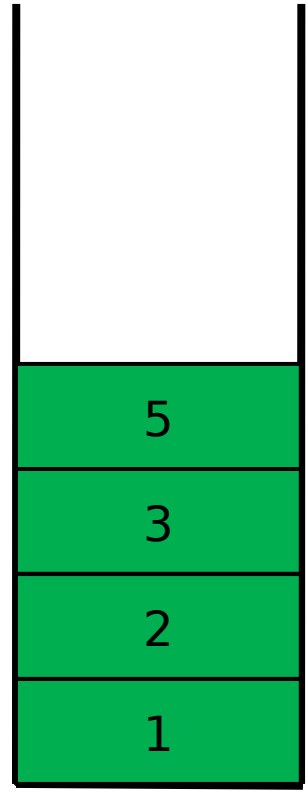
DFS



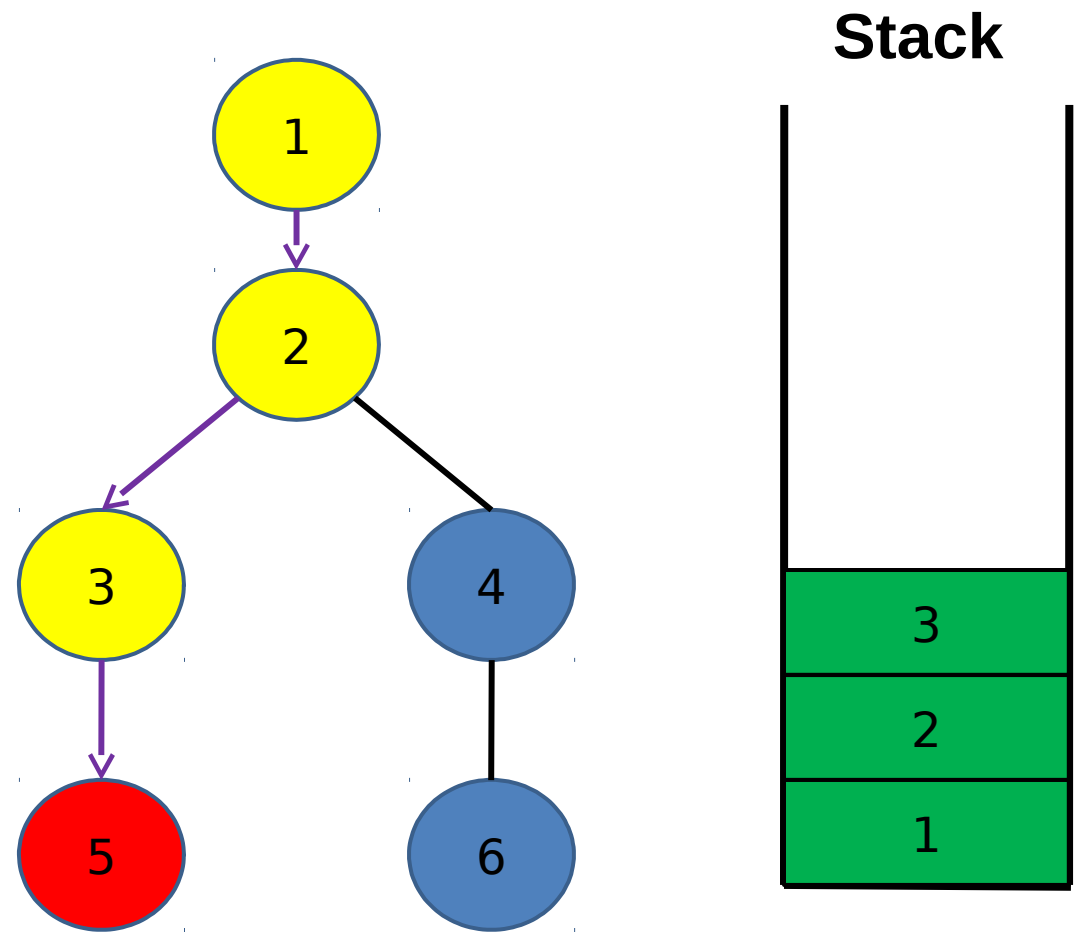
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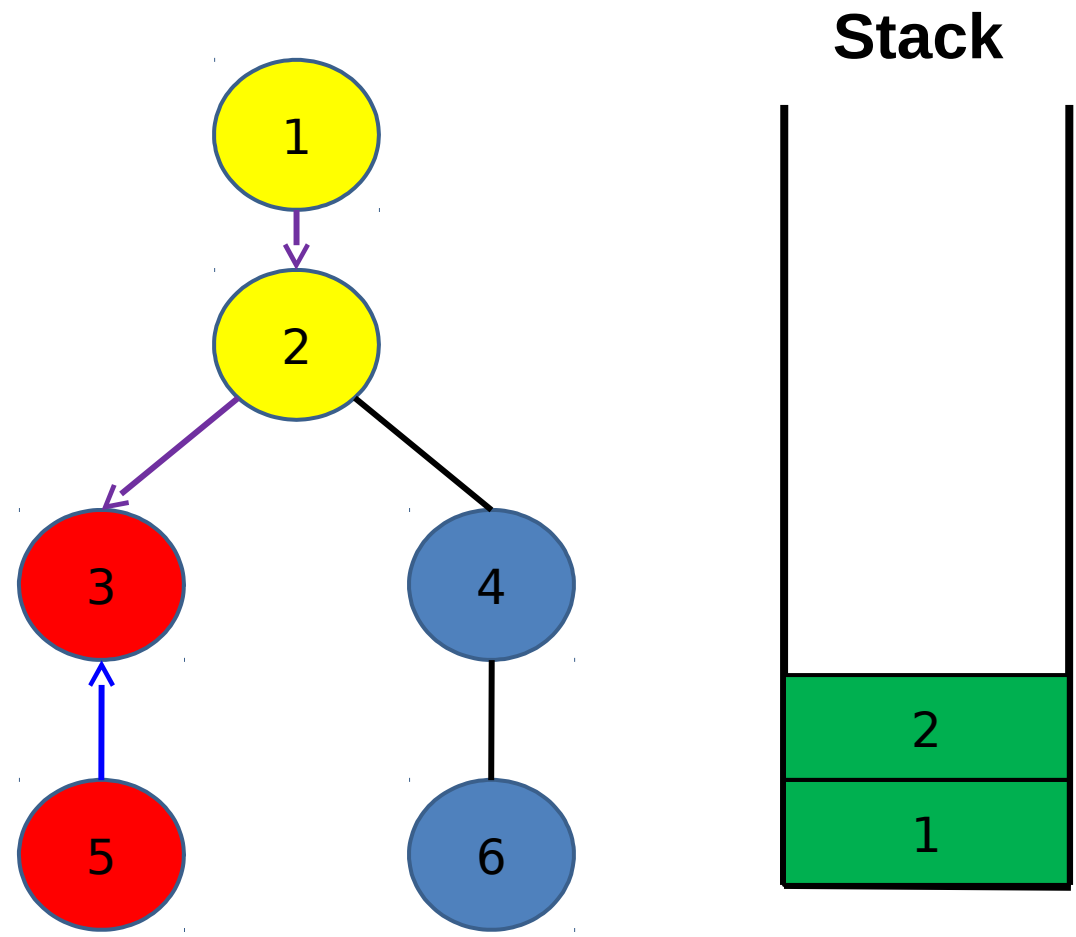
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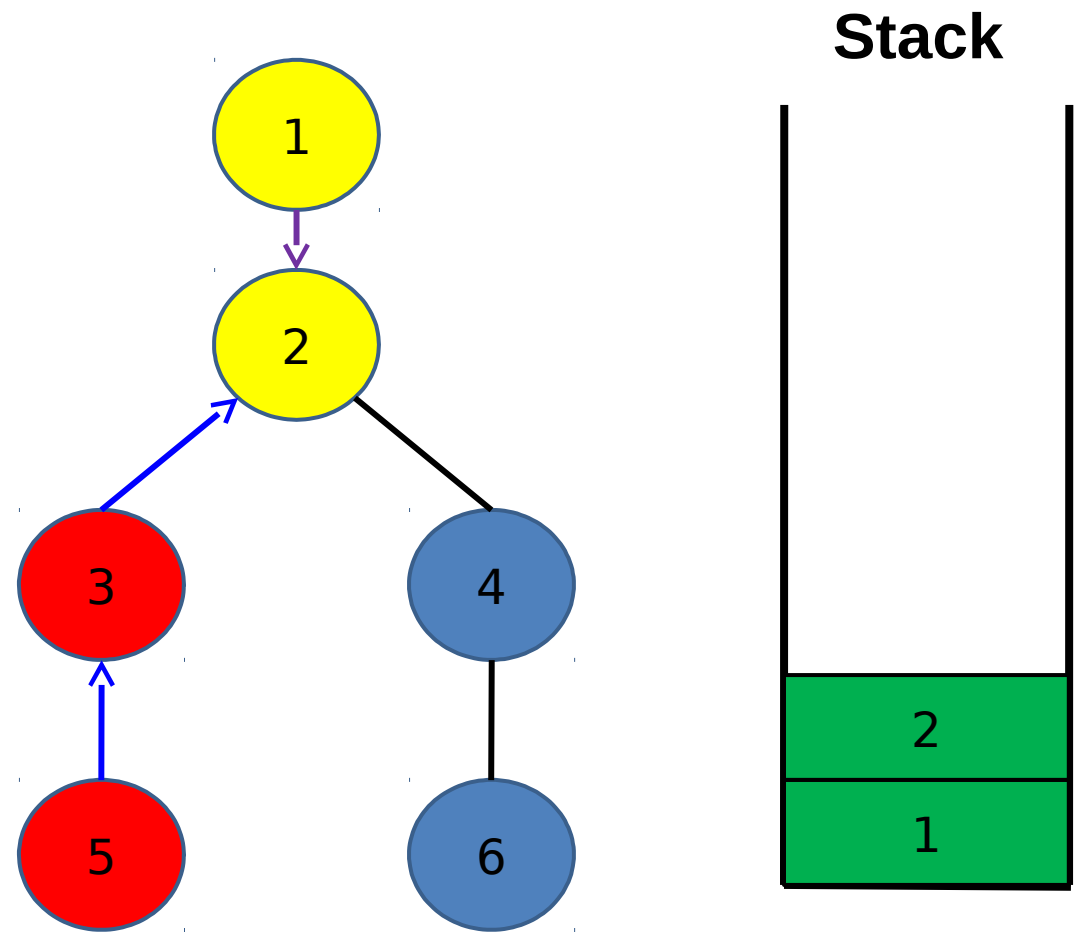
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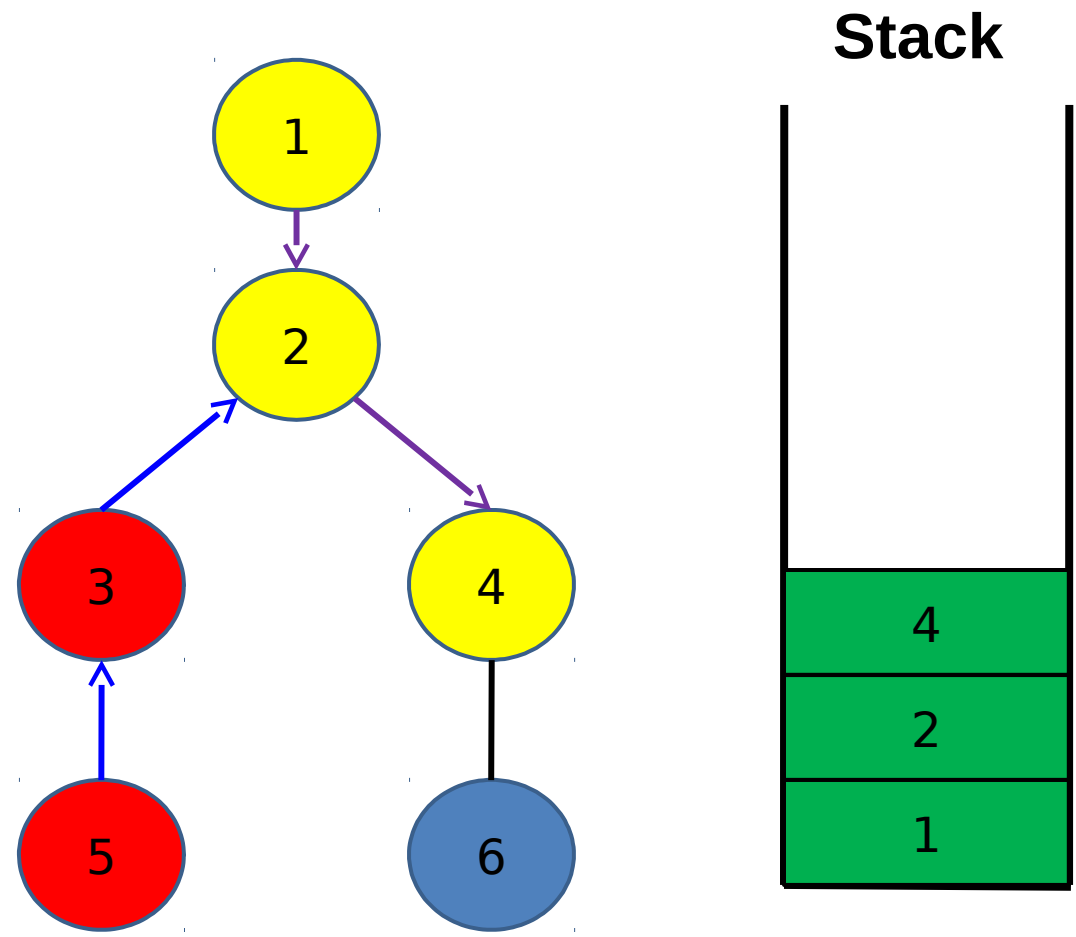
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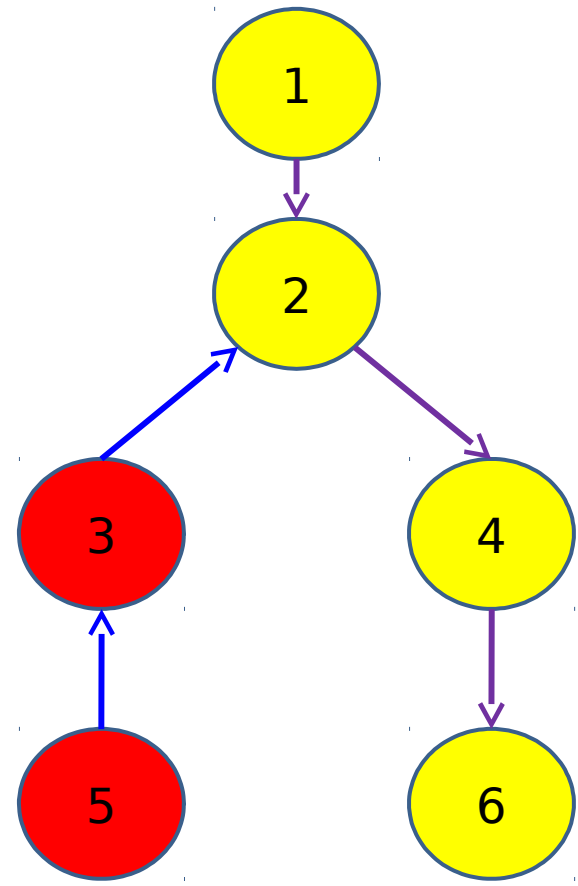
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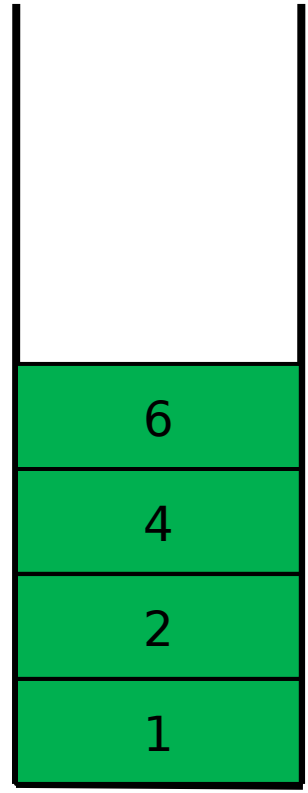
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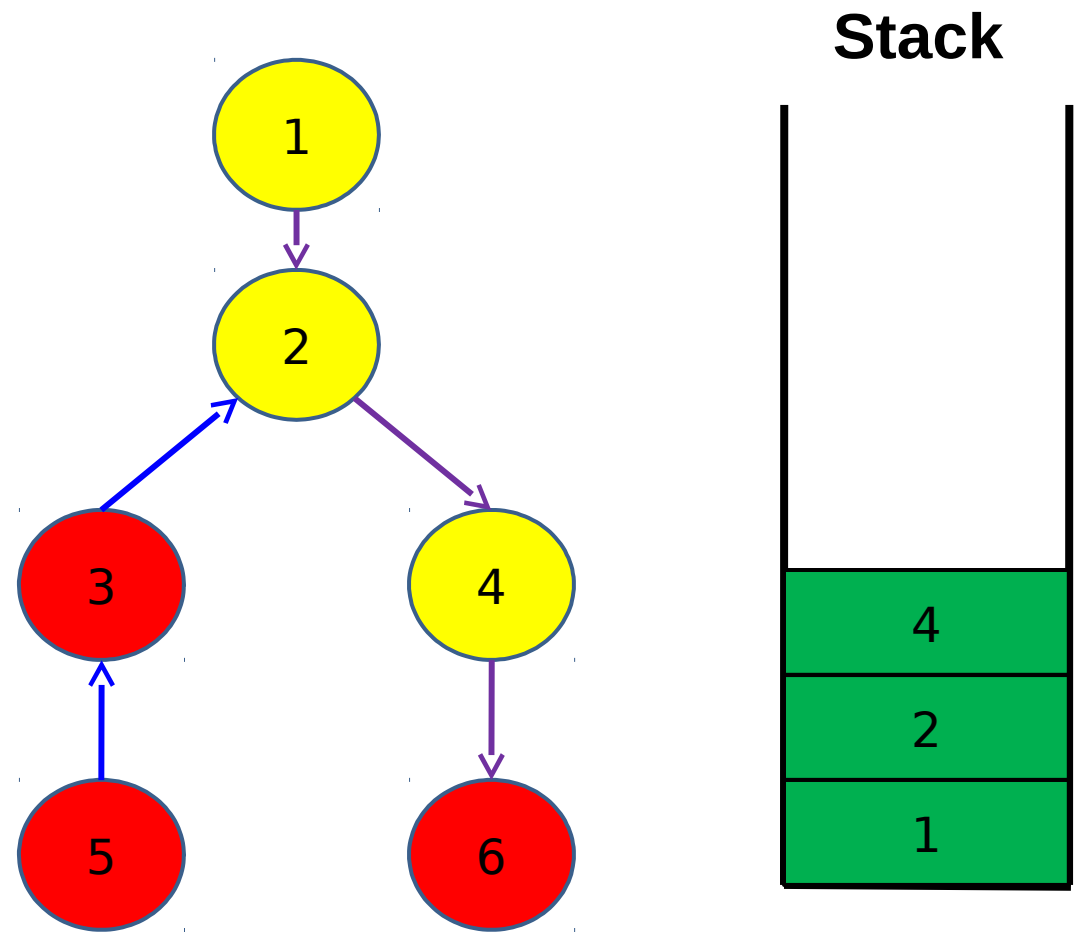
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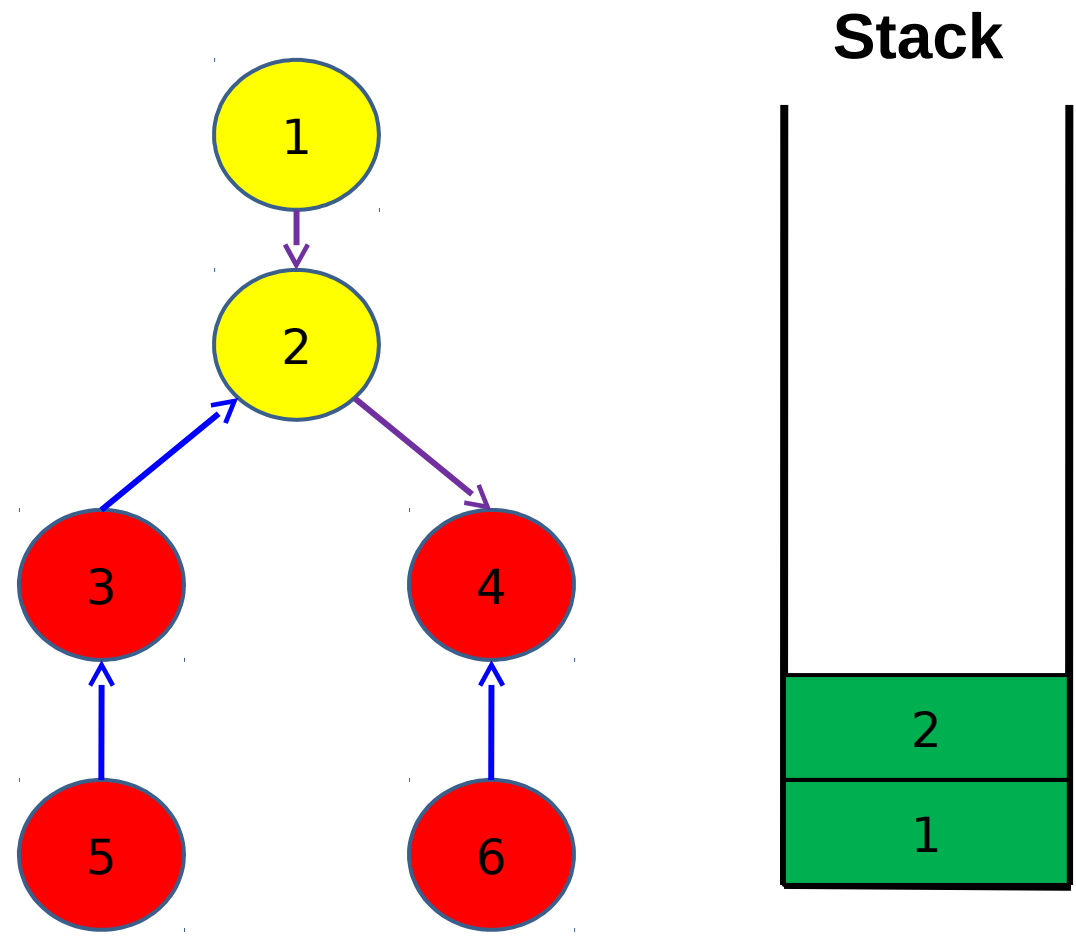
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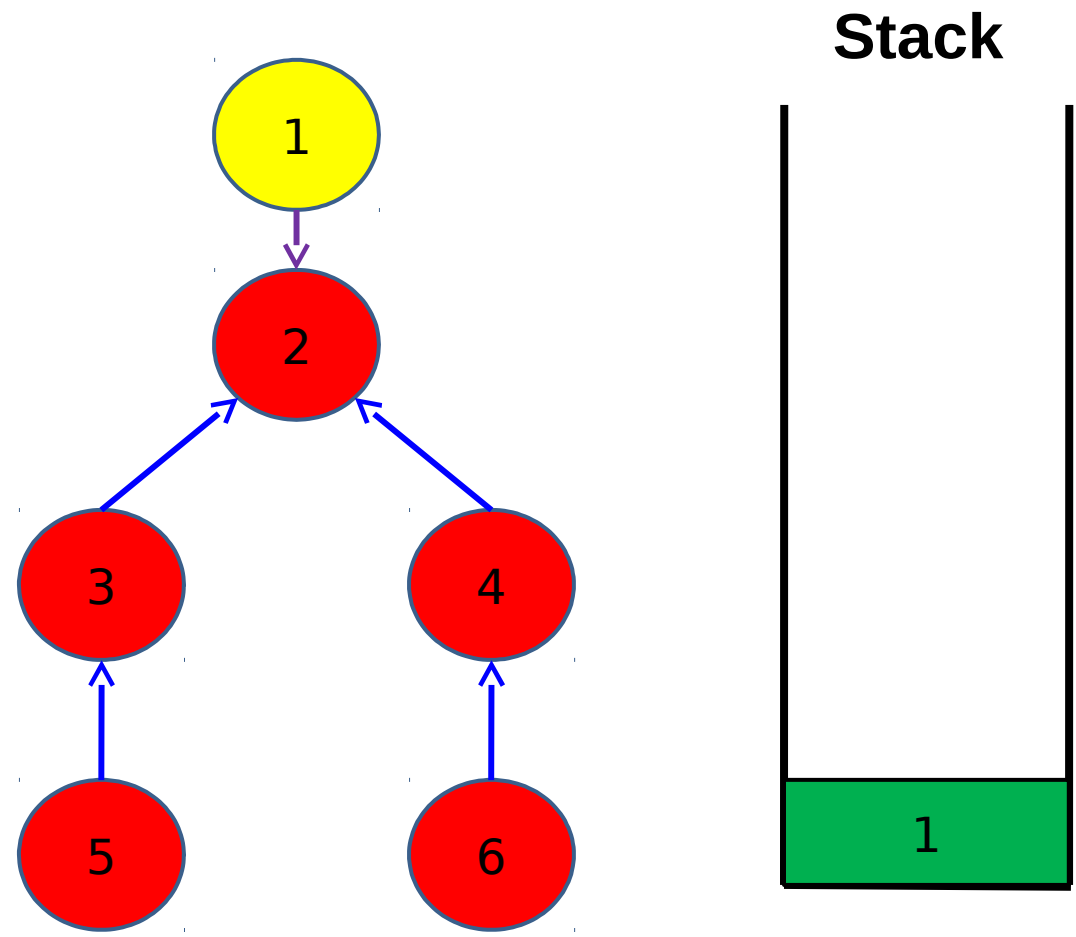
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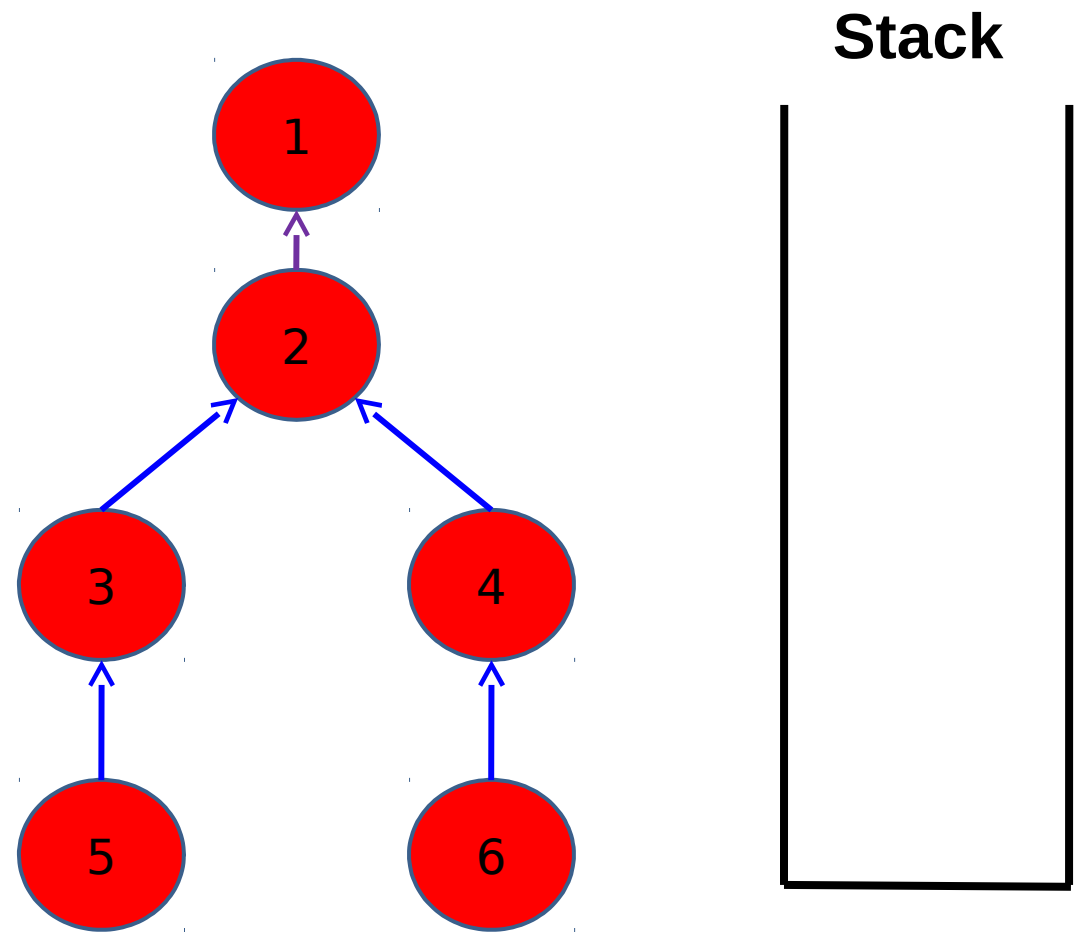
DFS



DFS



DFS



DFS

- Source Code(adjacency list)

```
void DFS(int cur)
{
    vis[cur]=true;

    for(int i=0;i<adj[cur].size();i++)
    {
        int next=adj[cur][i];
        if(!vis[next])
            DFS(next);
    }
    return;
}
```



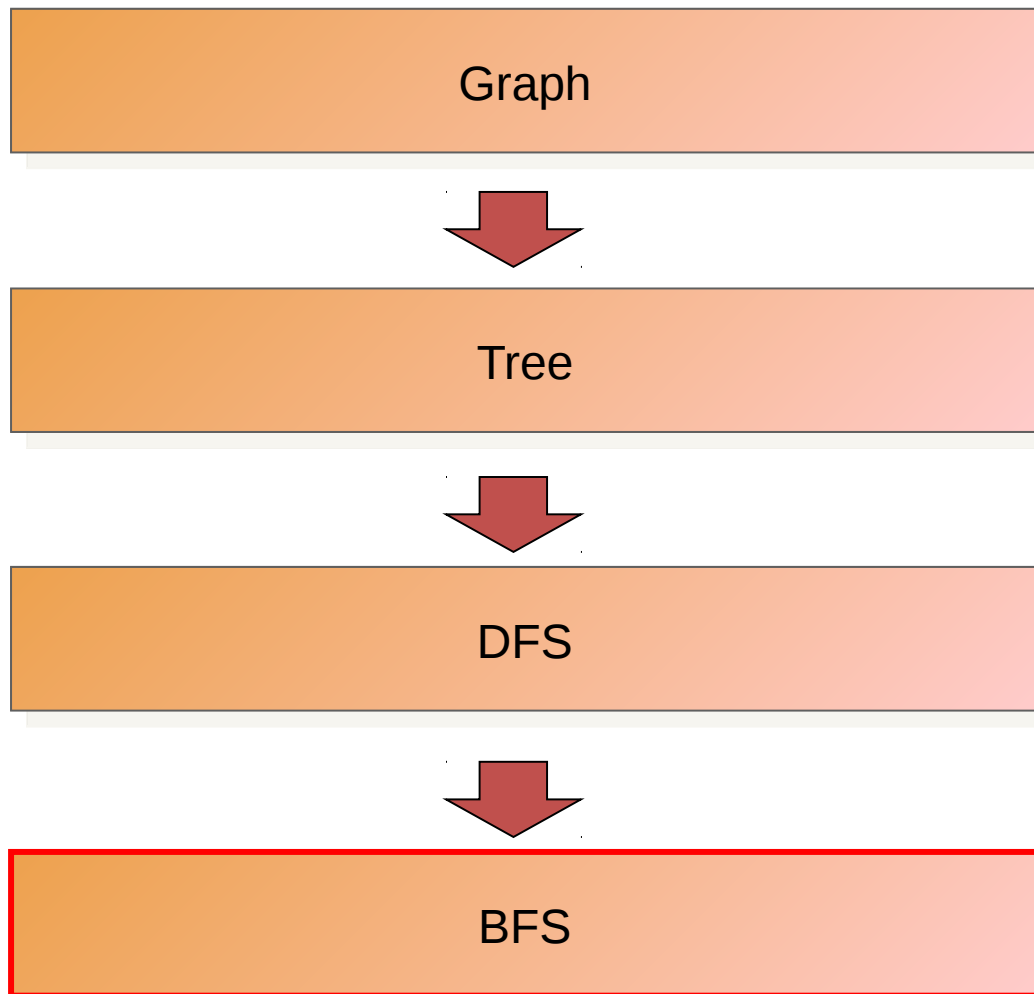
DFS

- Practice

[UVA-572] Oil Deposits



Outline



BFS

(B)readth-(F)irst-(S)earch



BFS

(B)readth-(F)irst-(S)earch

Queue

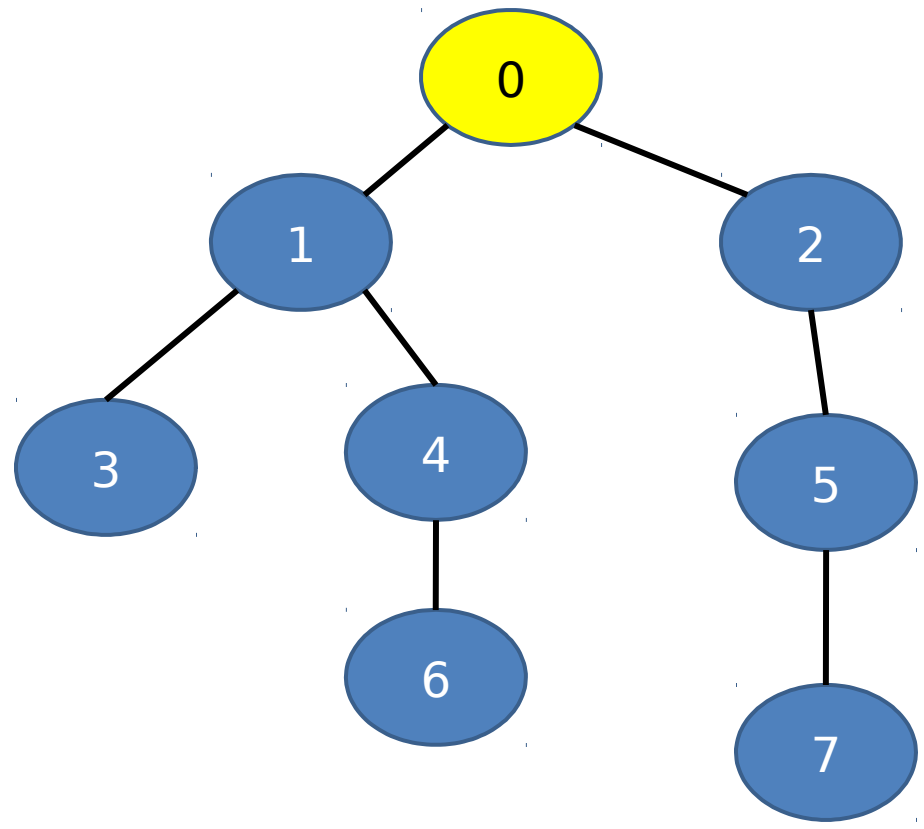




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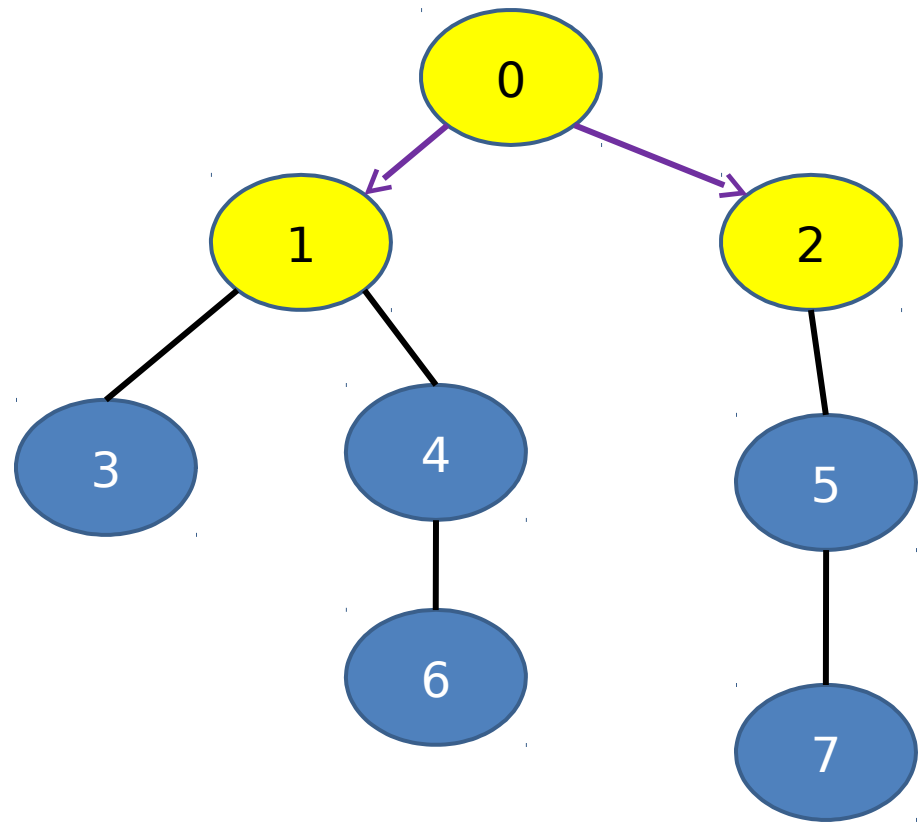
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BFS

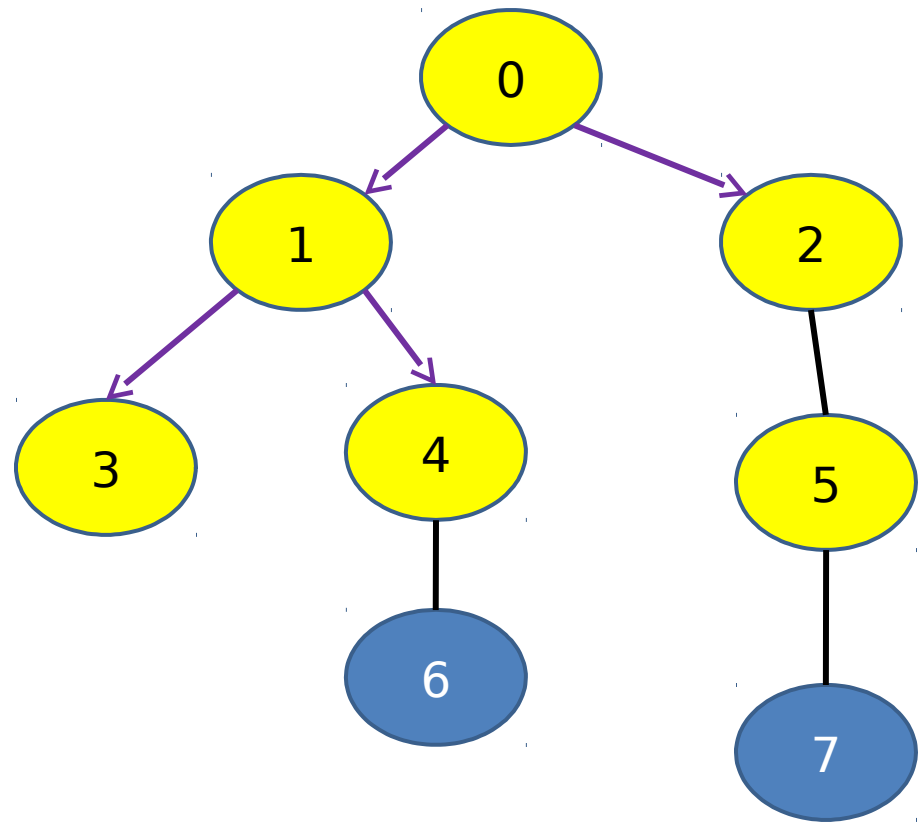


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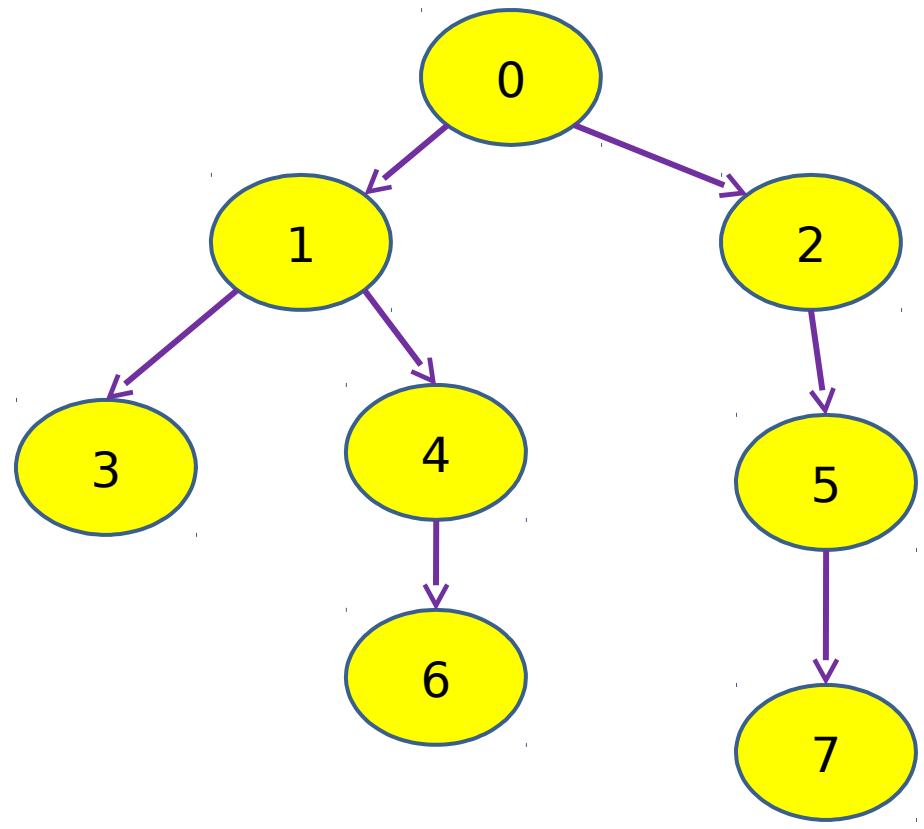
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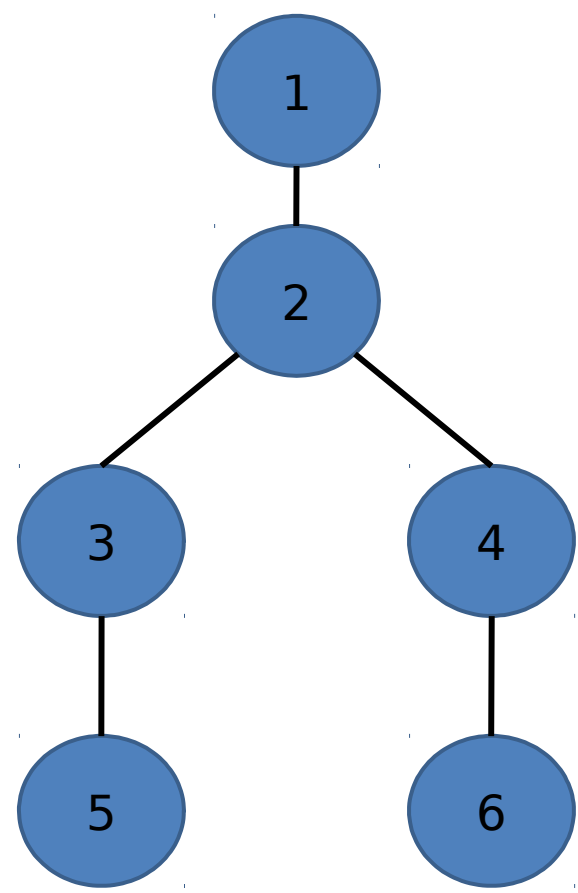
BFS



BFS



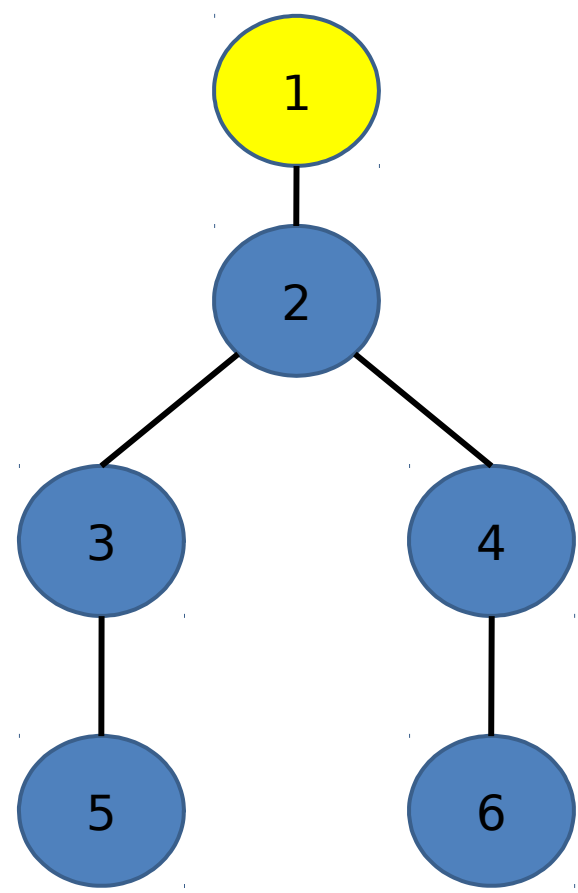
BFS



Queue



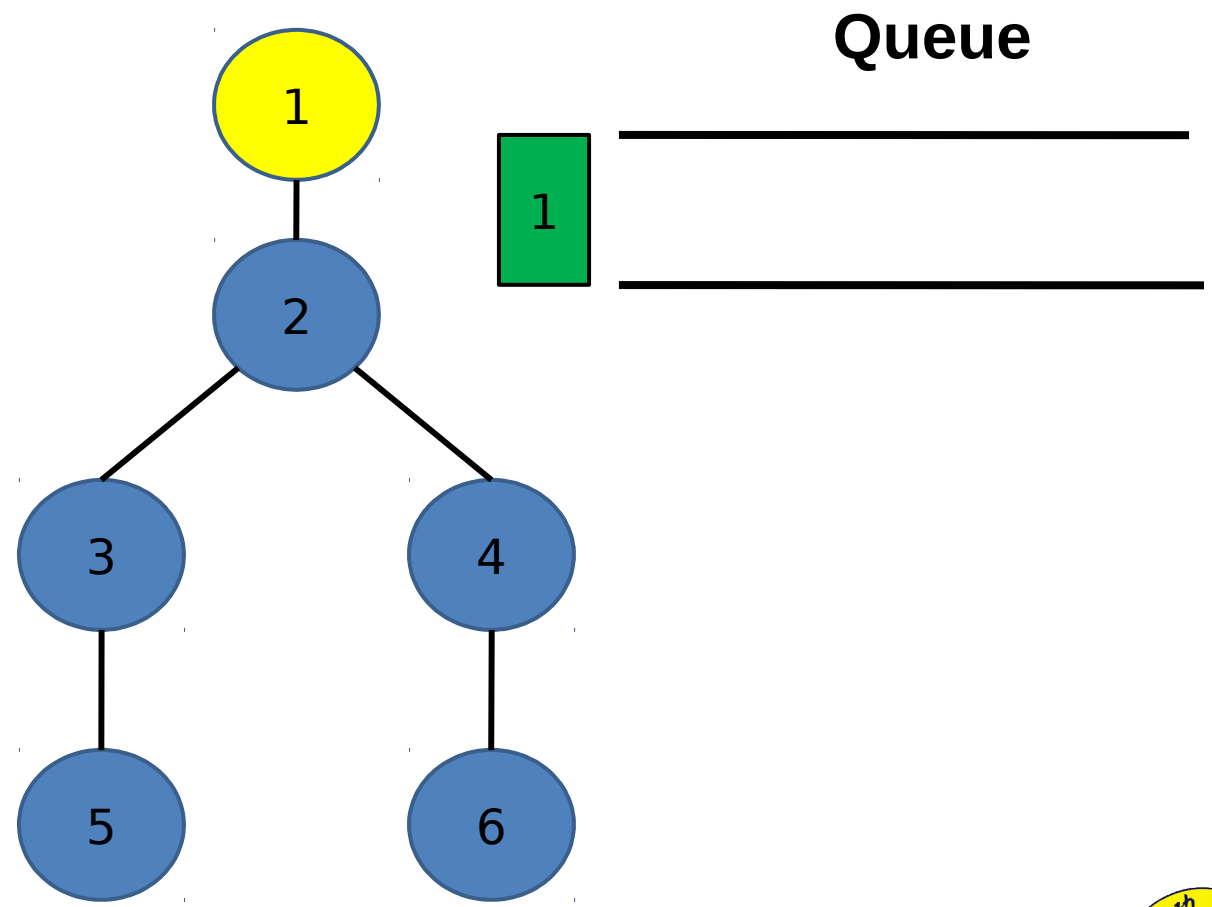
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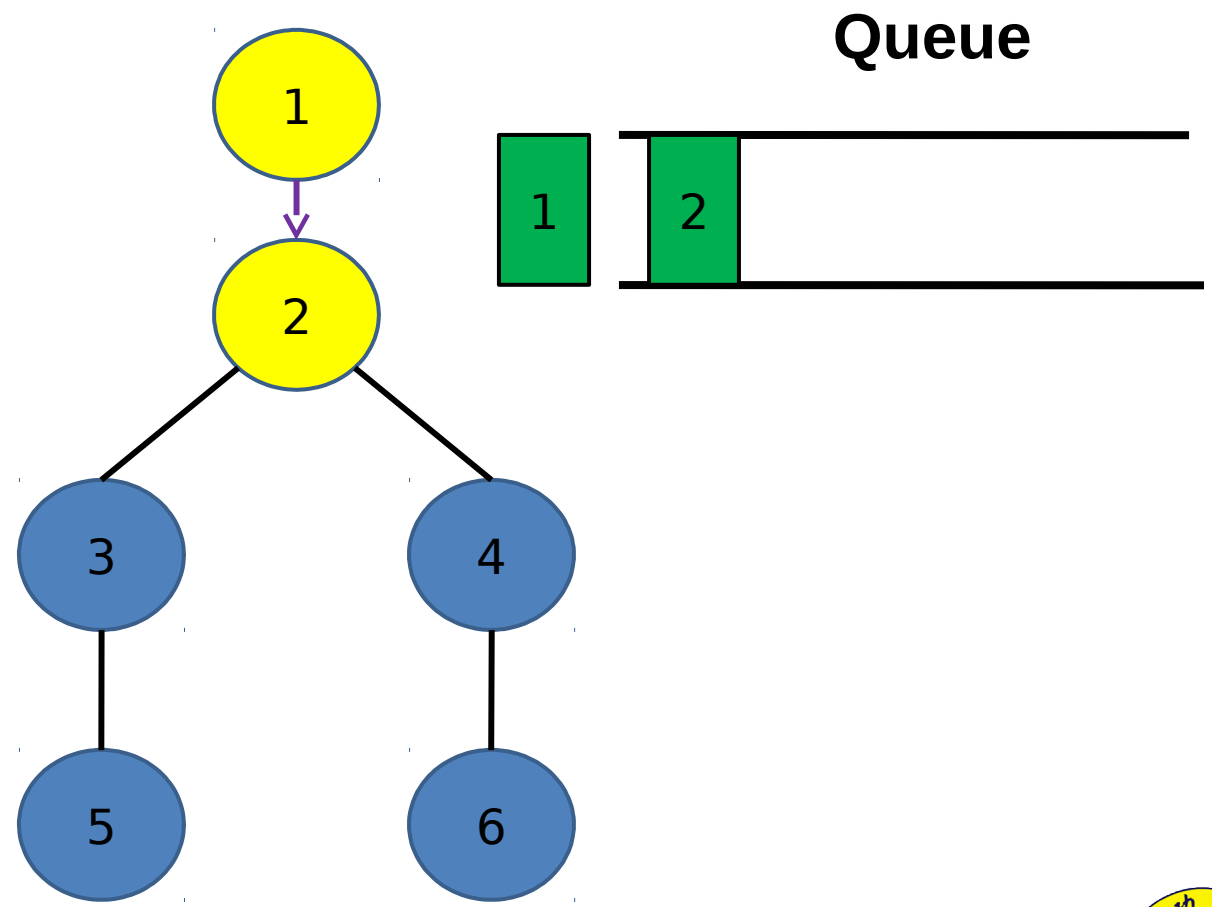
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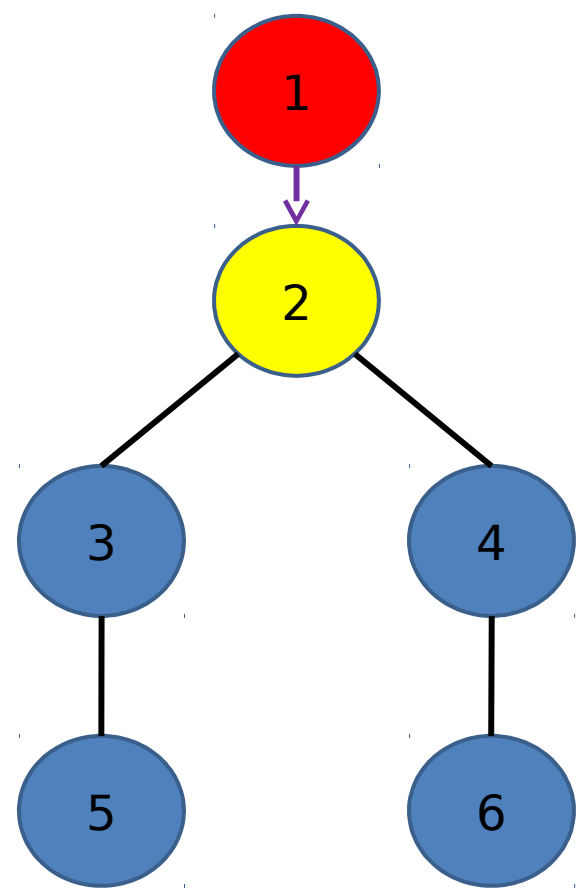
BFS



BFS



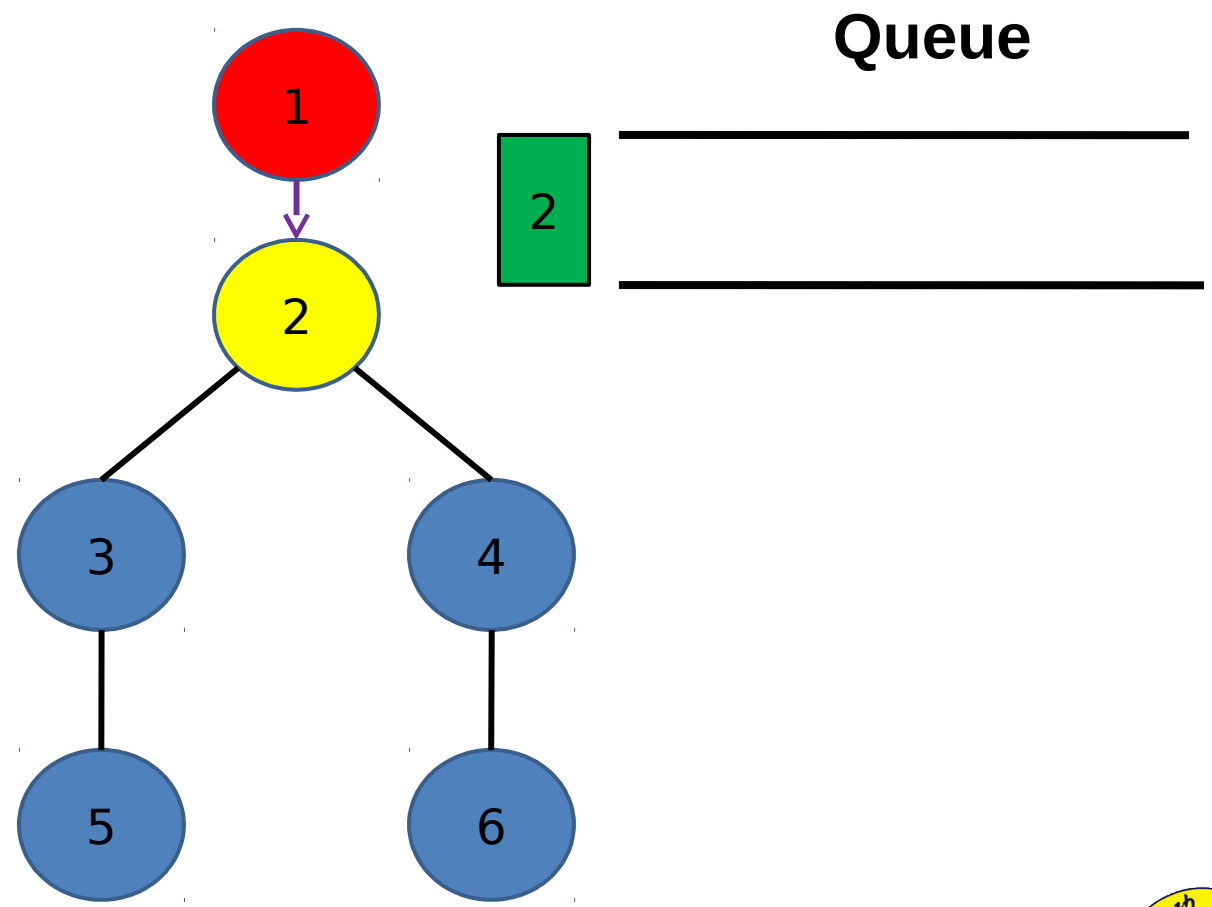
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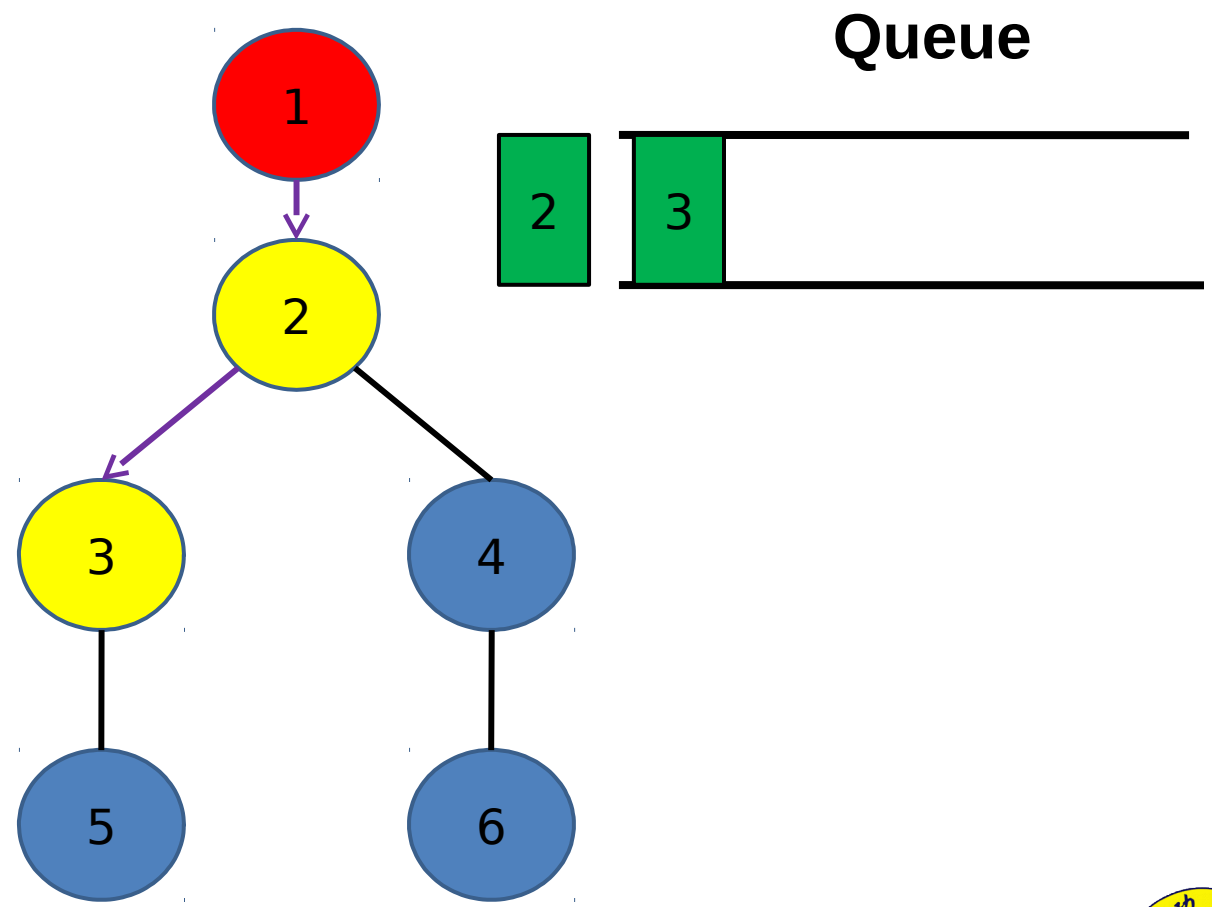
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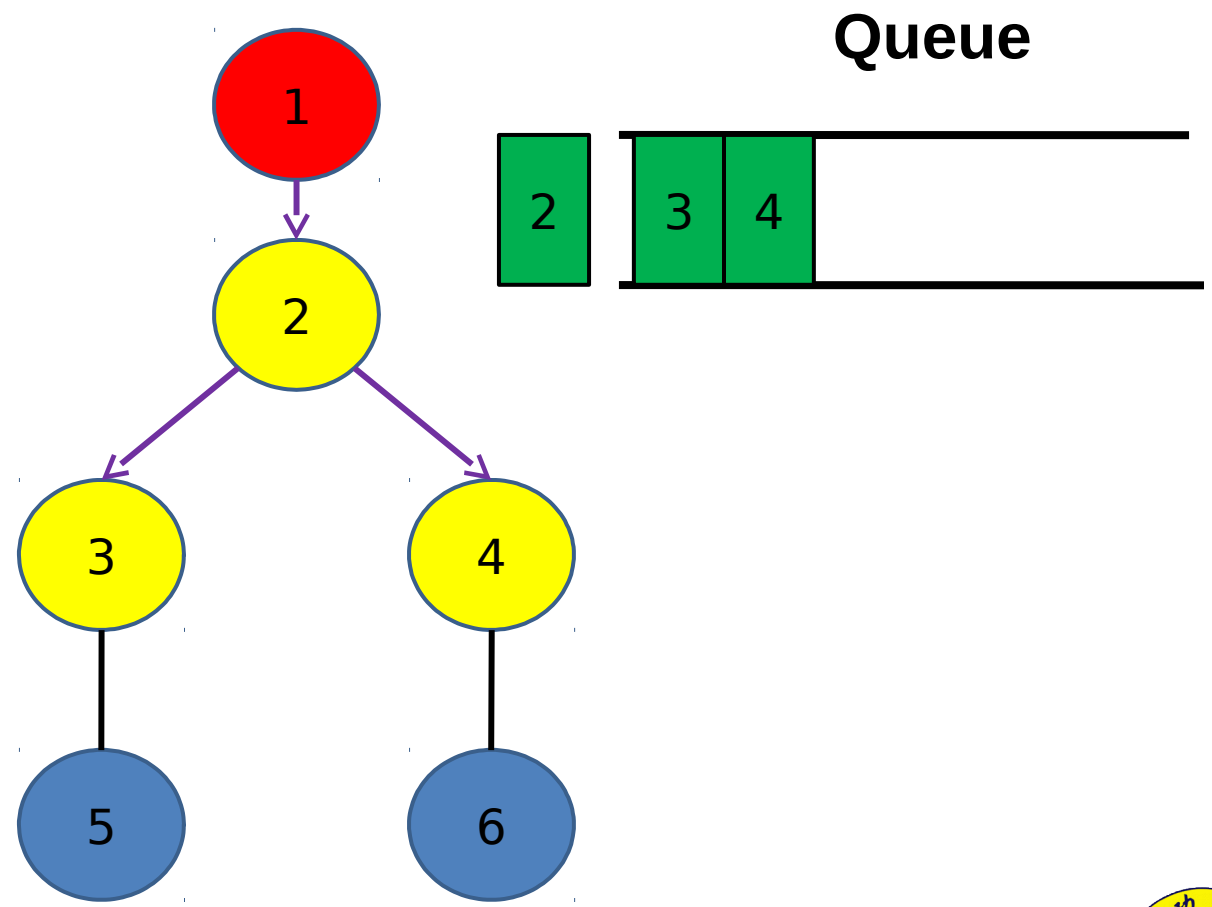
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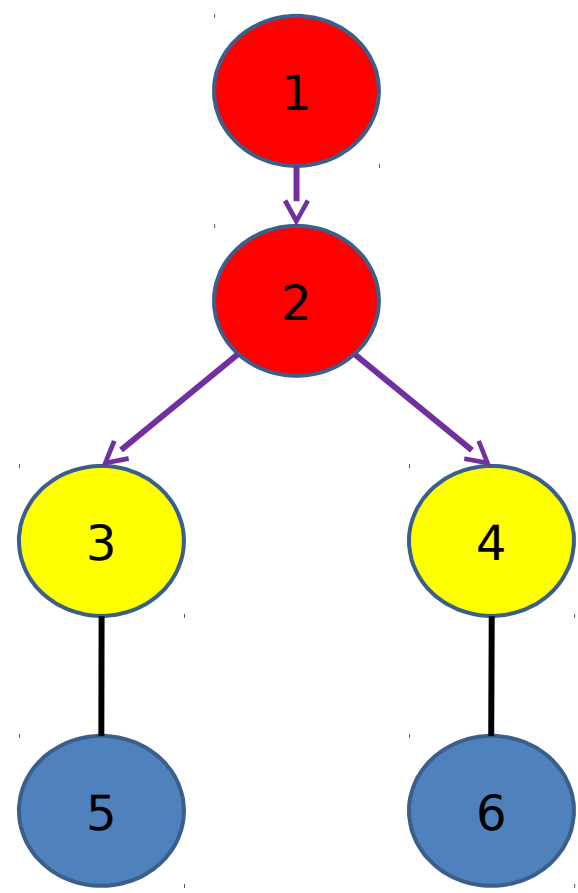
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BFS



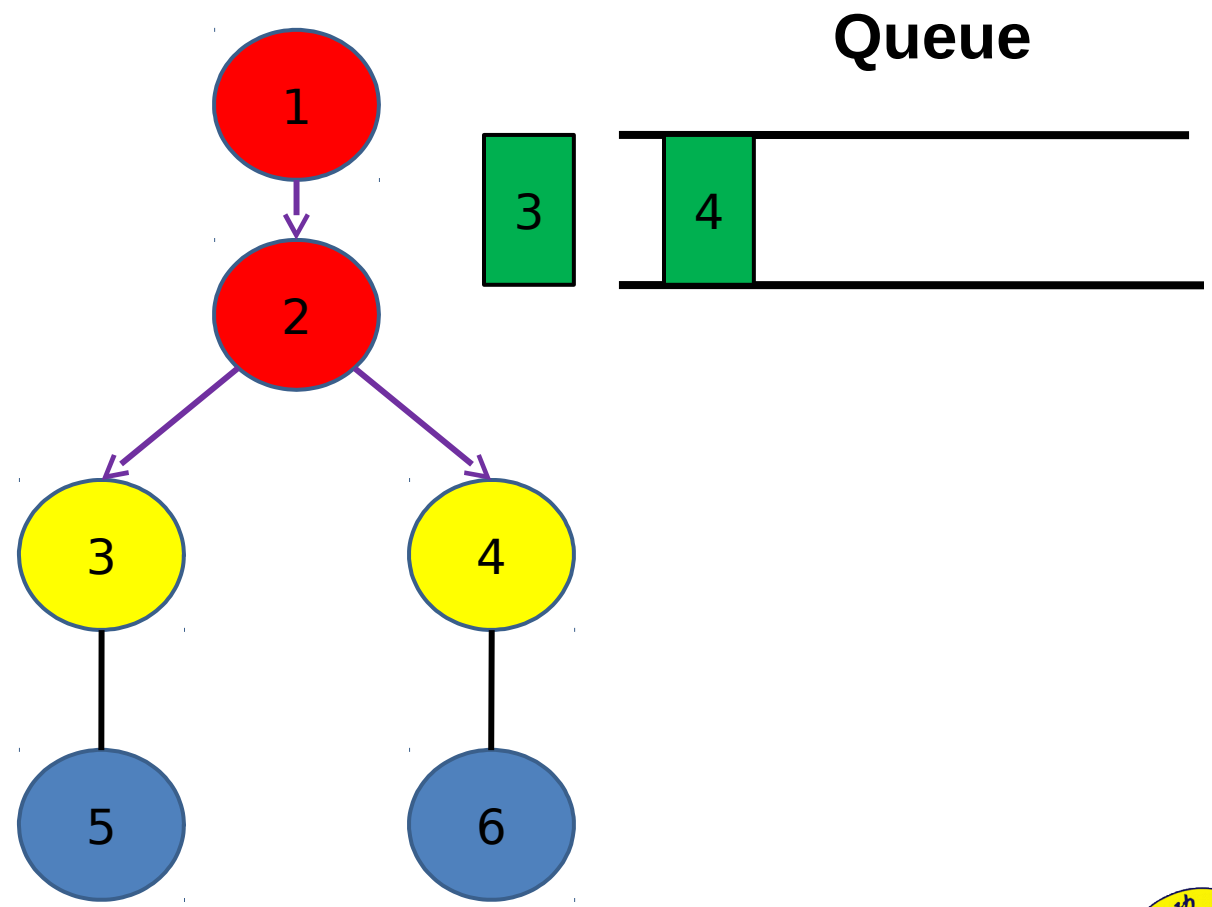
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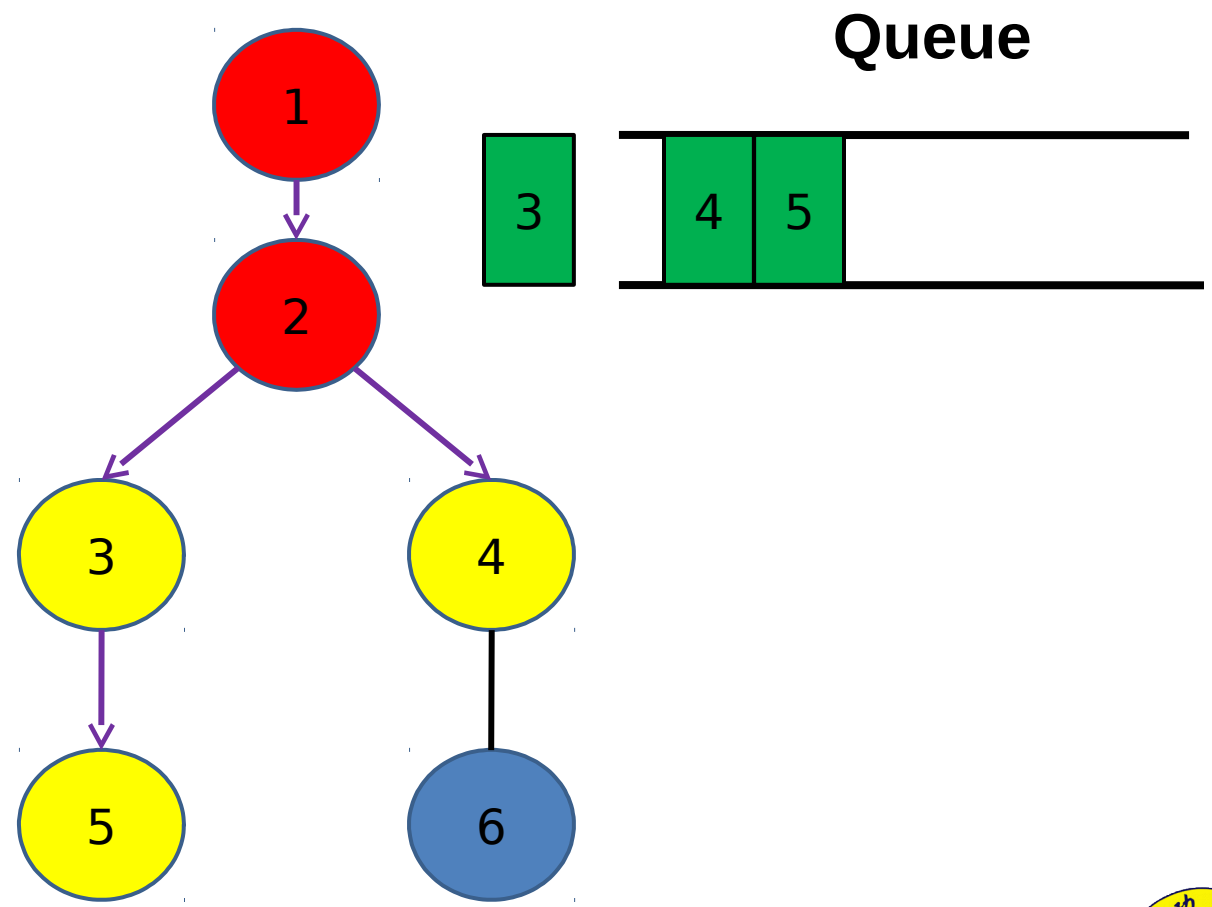
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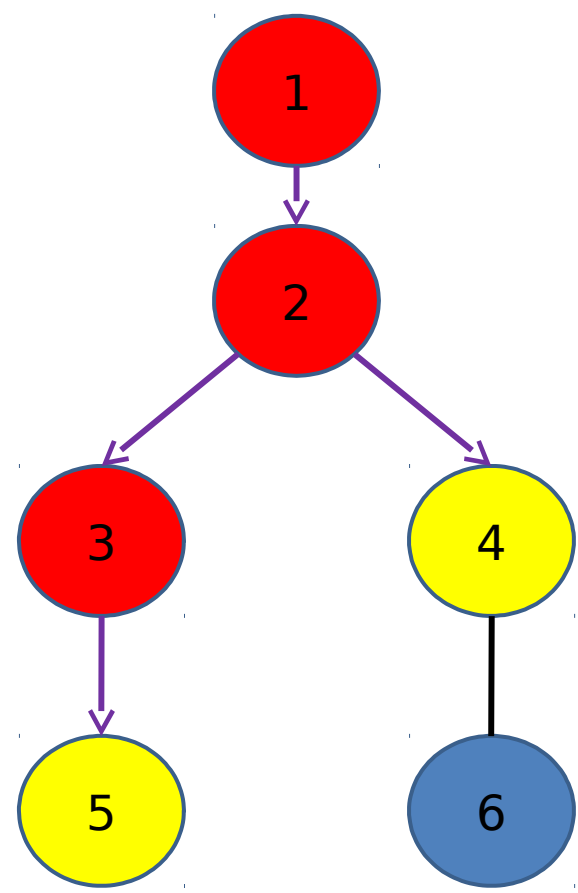
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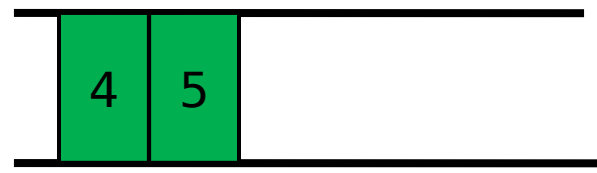
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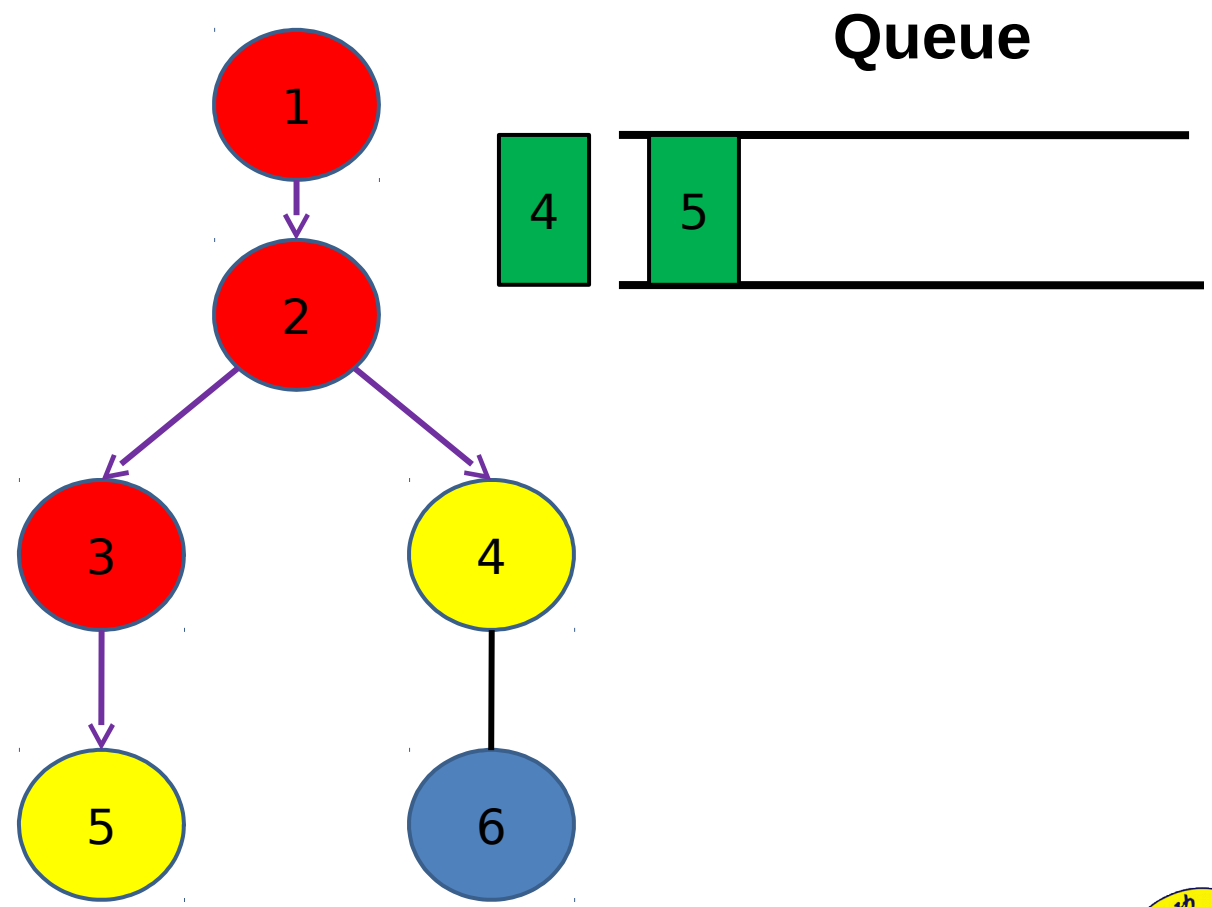
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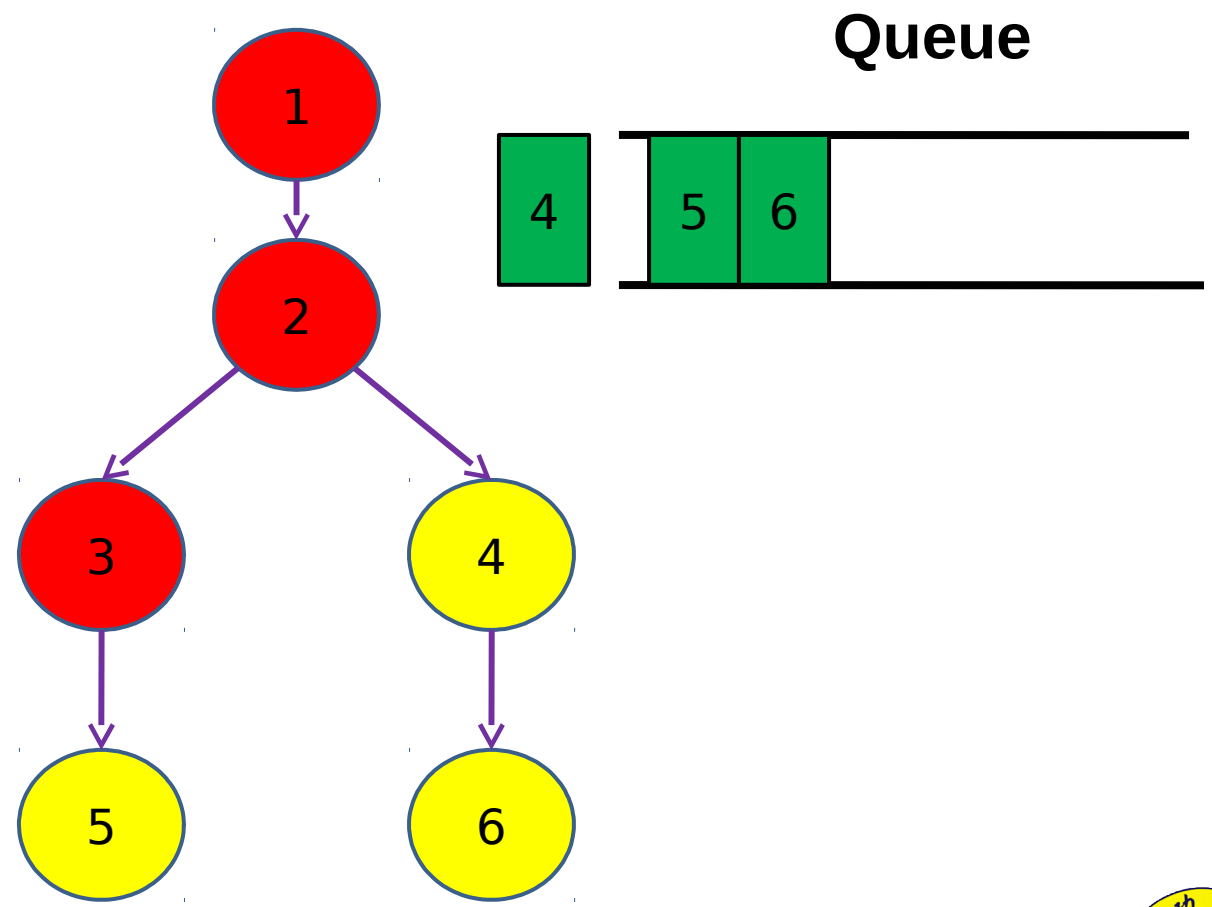
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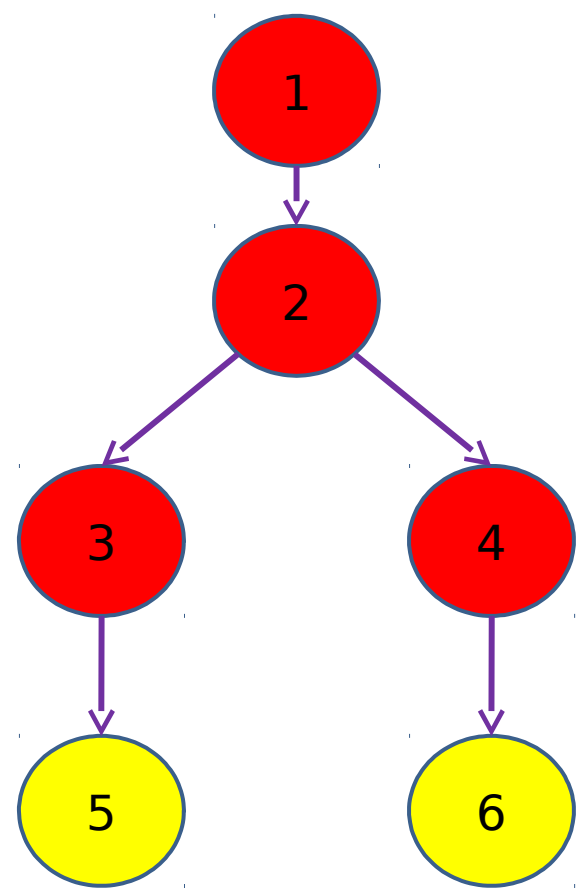
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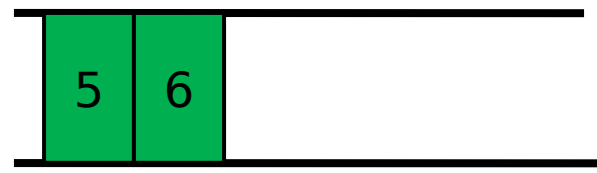
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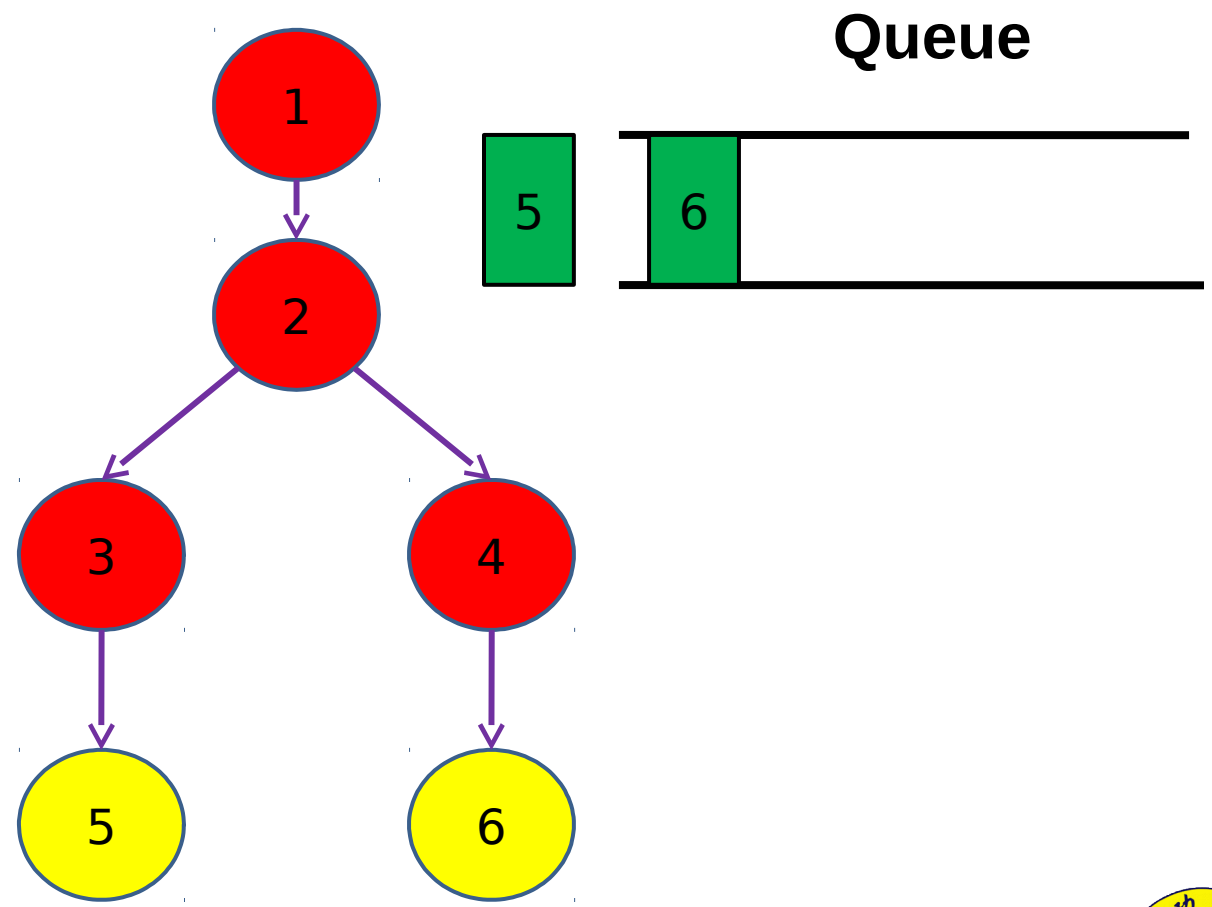
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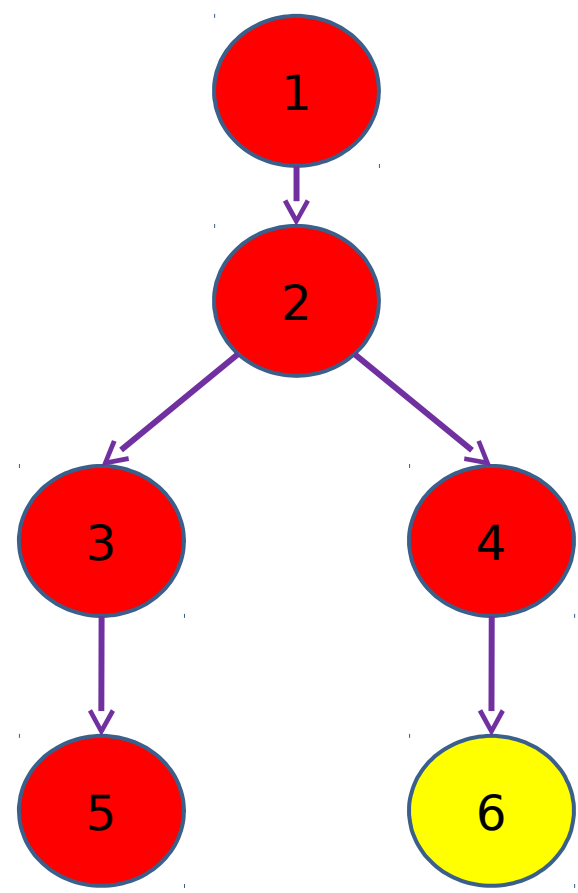
Queue



BFS



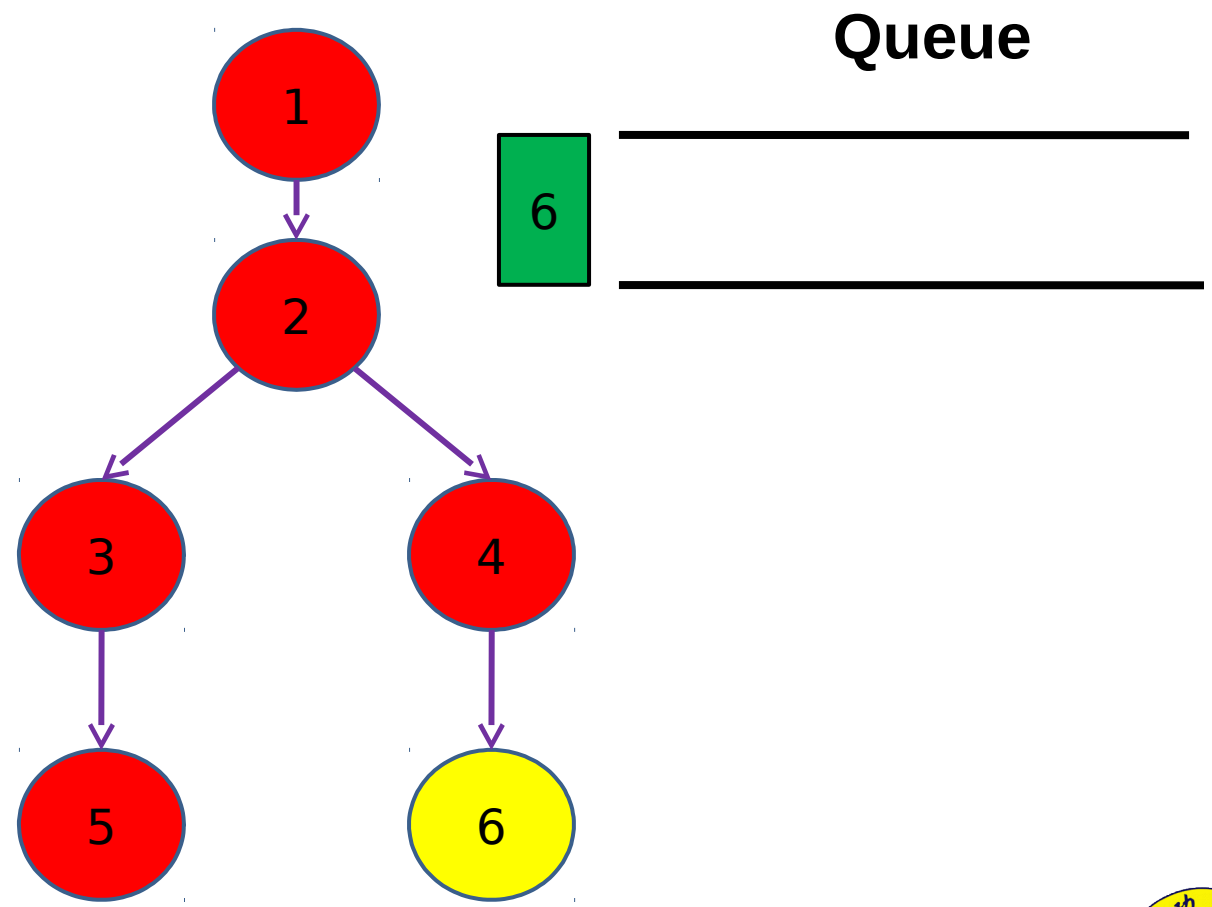
BFS



Queue

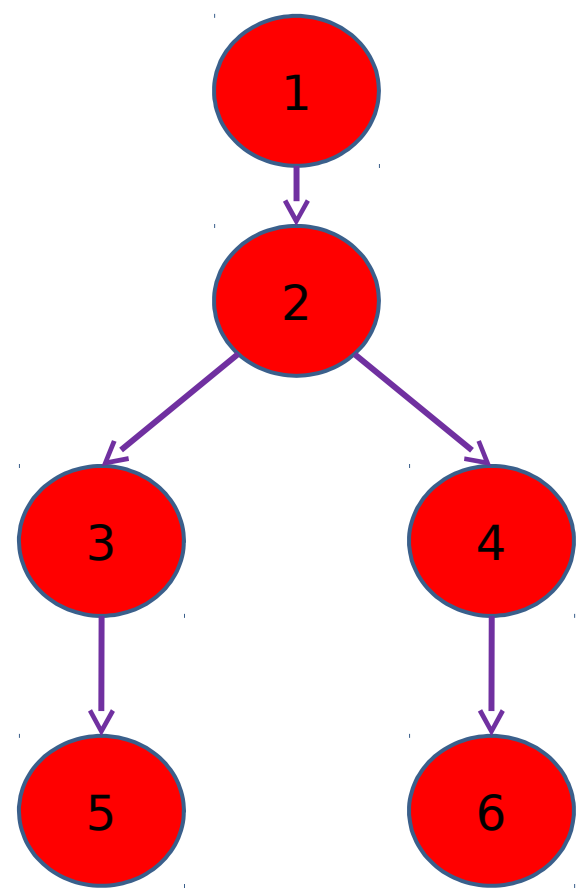


BFS



BFS

Queue



BFS

- Source Code (adjacency list)

```
void BFS(int root)
{
    queue<int> que;
    que.push(root);
    visited[root]=true;

    while(!que.empty())
    {
        int cur=que.front();
        que.pop();

        for(int i=0;i<adj[cur].size();i++)
        {
            int next=adj[cur][i];
            if(!visited[next])
            {
                visited[next]=true;
                que.push(next);
            }
        }
    }
    return;
}
```



BFS

- Practice

[UVA-532] Dungeon Master



- **Skill:**

```
int dir[4][2]={ {1,0},{-1,0},{0,1},{0,-1} }
```

☒ search four directions



- Skill:

```
int dir[4][2]={ {1,0},{-1,0},{0,1},{0,-1} };  
  
void DFS(int cur_x,int cur_y)  
{  
    vis[cur_x][cur_y]=1;  
  
    for(int i=0;i<4;i++)  
    {  
        int nx=cur_x+dir[i][0];  
        int ny=cur_y+dir[i][1];  
  
        //watch for boundary  
        if( !vis[nx][ny])  
            DFS(nx,ny);  
    }  
}
```



Time Complexity

DFS $O(V + E)$

BFS $O(V + E)$

V: the number of nodes

E: the number of edges

(adjacency list)



Time Complexity

DFS $O(V^2)$

BFS $O(V^2)$

V: the number of nodes

E: the number of edges

(adjacency matrix)



HW3

Totally 30 problems

UVa:

260,336,352,383,439,532,539,567,571,601,705,

762,10004,10009,10474, 10505,10592,10603, 10946, 11624, 532, 572

POJ:

1129,1154,1416,1606,1753,1915,1979,2243



Thank for Your Attention

